

# PARASITE: PAssword Recovery Attack against Srp Implementations in ThE wild

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Mohamed Sabt

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# Context and Motivations

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# A Few Words About PAKEs

What to expect from a PAKE, starting from a password:

- Authentication
- End up with strong key
- Resist to (offline) dictionary attack

Lots of different PAKEs (two main families: balanced - asymmetric).

# Why Looking at PAKEs?

Recent interest (WPA3 and CFRG competition after patents expiration) with practical security considerations

- Dragonfly and WPA3: Dragonblood<sup>1</sup> and attack refinement<sup>2</sup>
- Partitioning Oracle Attack<sup>3</sup> applied to some OPAQUE implementations

Small leakage can be devastating

Case study: Secure Remote Password

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<sup>1</sup> M.Vanhoef and E.Ronen *Dragonblood: Analyzing the Dragonfly Handshake of WPA3 and EAP-pwd*. In IEEE S&P. 2020

<sup>2</sup> D.Braga et al. *Dragonblood Is Still Leaking: Practical Cache-based Side-Channel in the Wild*. In ACSAC. 2020

<sup>3</sup> J.Len et al. *Partitioning Oracle Attack*. In USENIX Security. 2021

# What about SRP?

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Available for a long time => de facto standard for more than 20 years

What about SRP implementations in the wild ?

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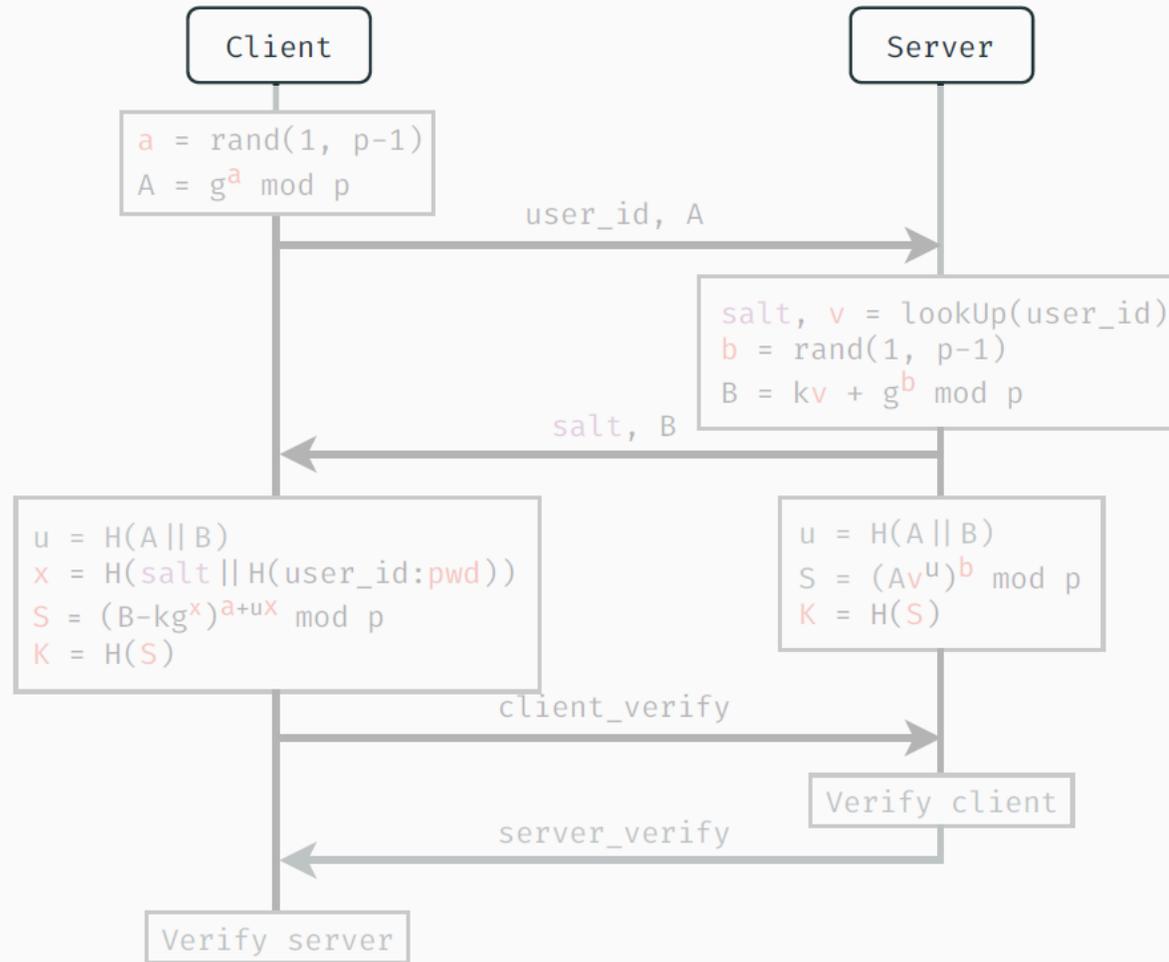
What about SRP implementations in the wild ?

- Recent work on SRP at ACNS<sup>1</sup>

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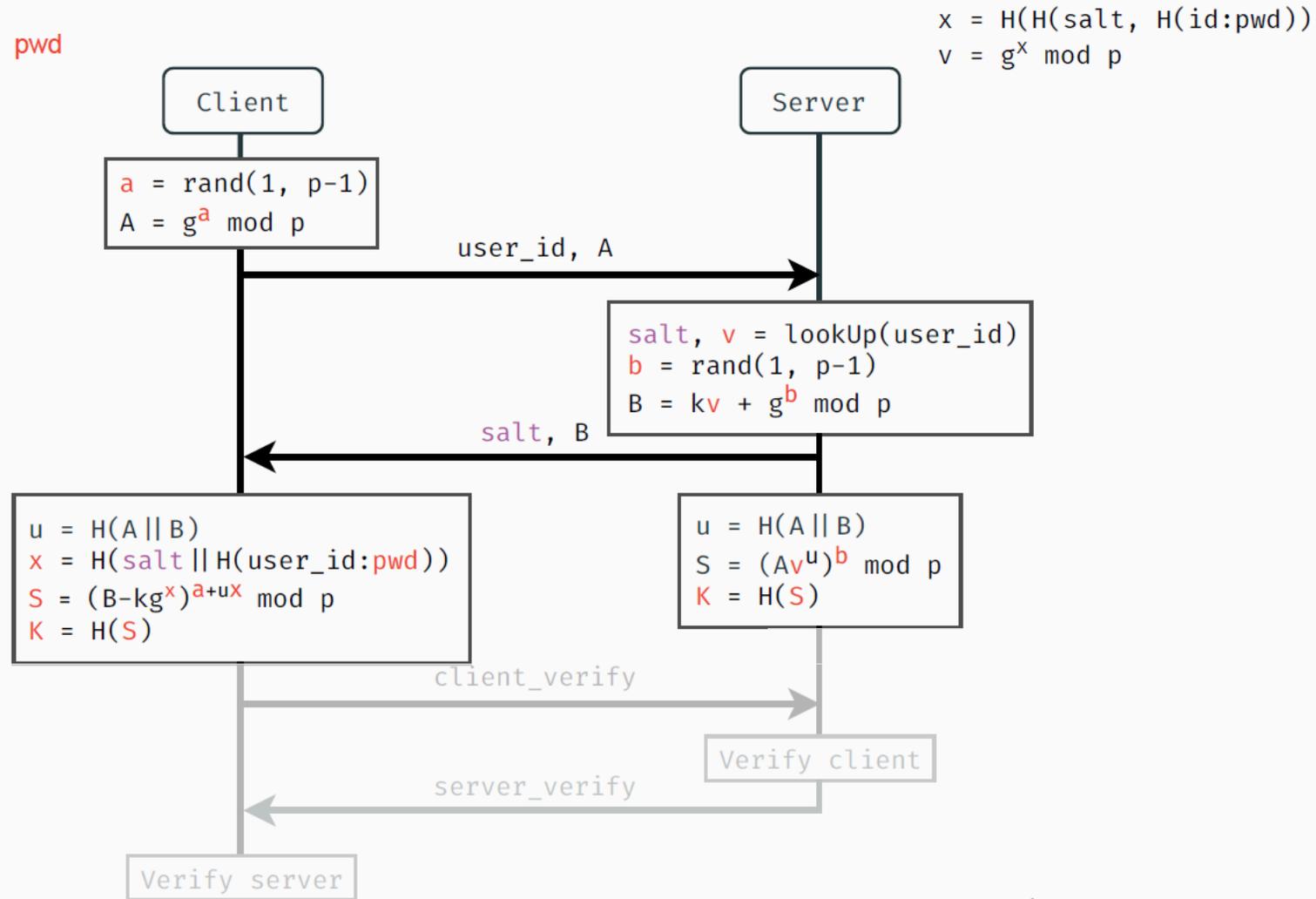
<sup>1</sup> A.Russon Threat for the Secure Remote Password Protocol and a Leak in Apple's Cryptographic Library. In ACNS. 2021

# SRP Protocol Overview

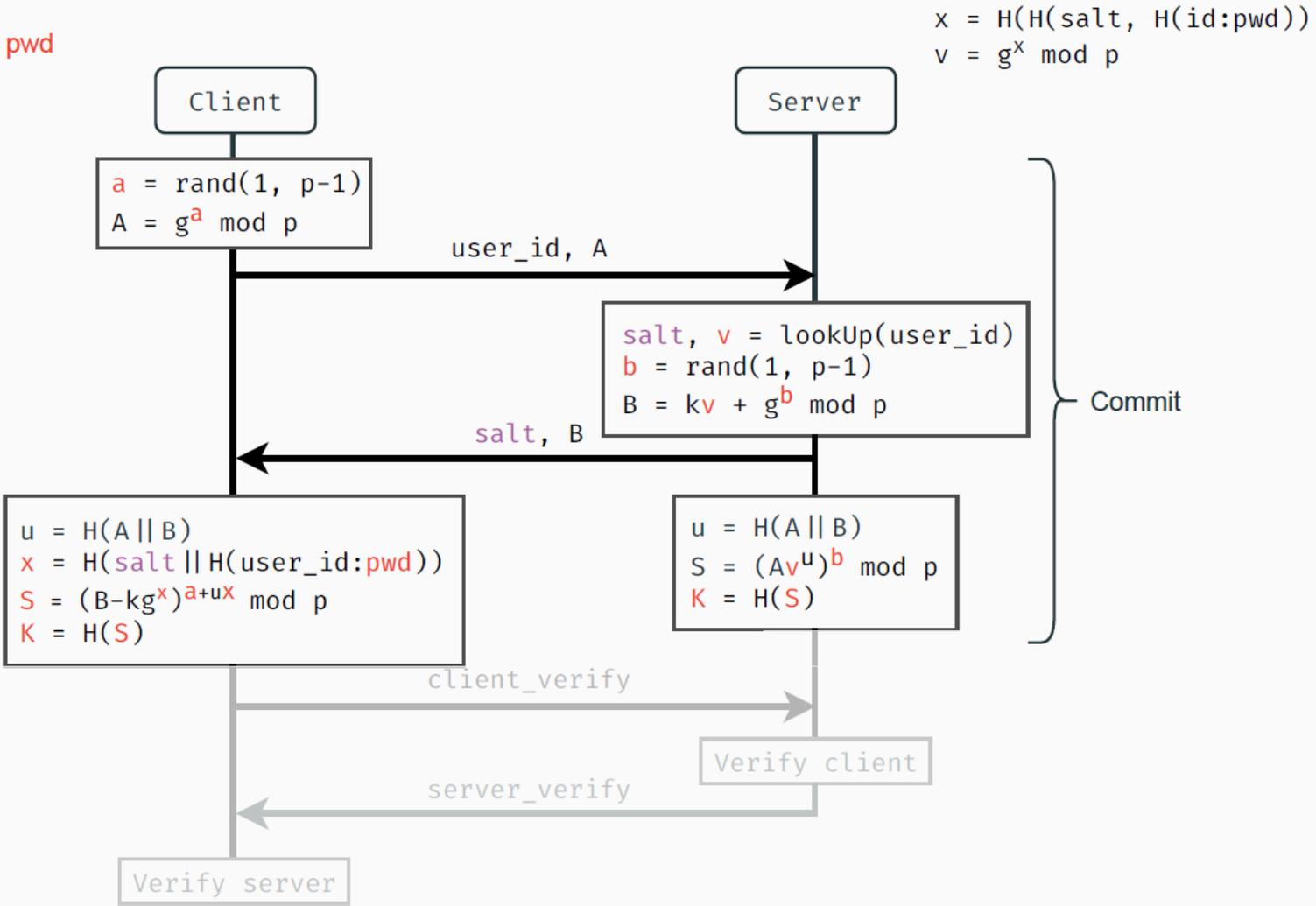




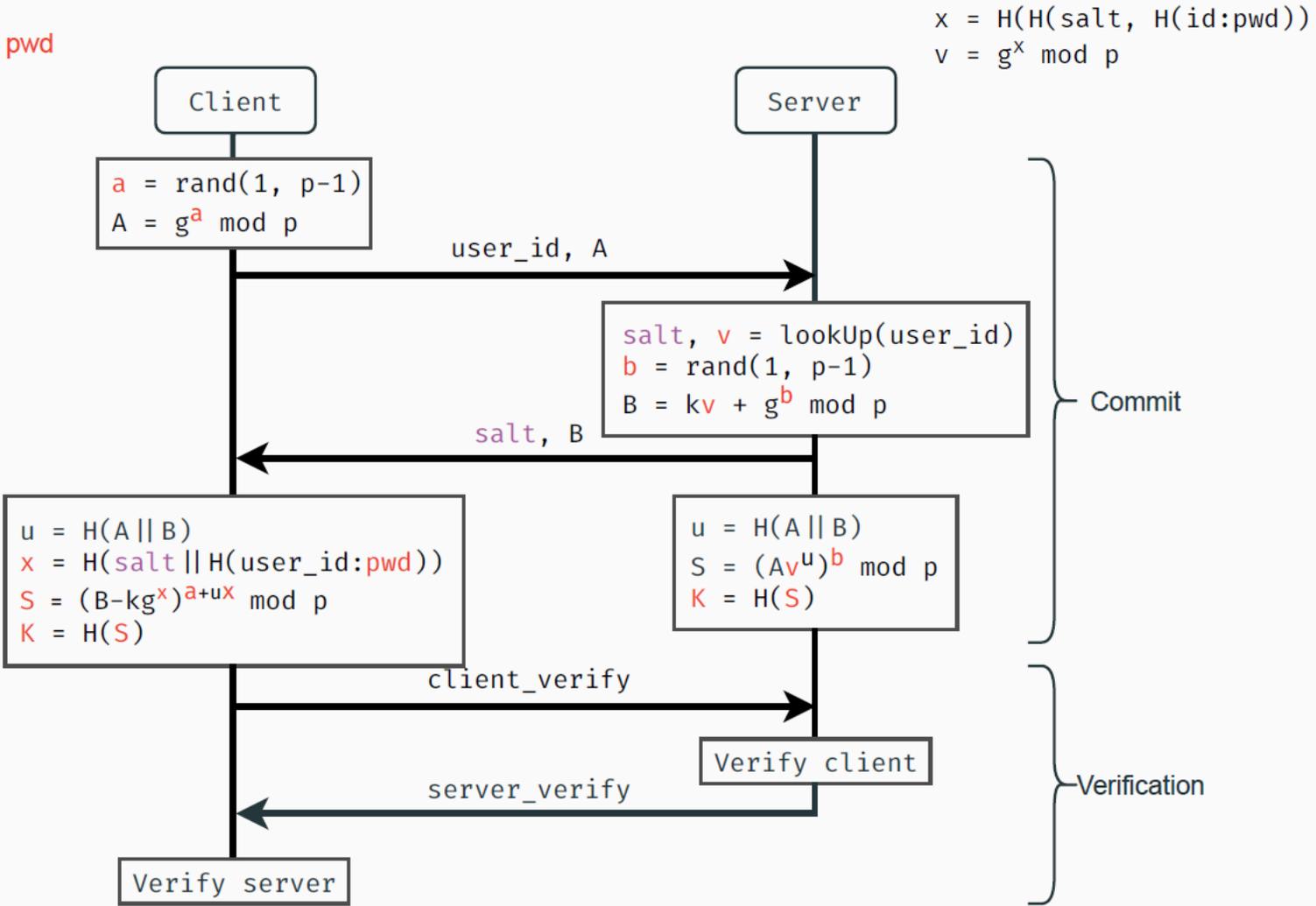
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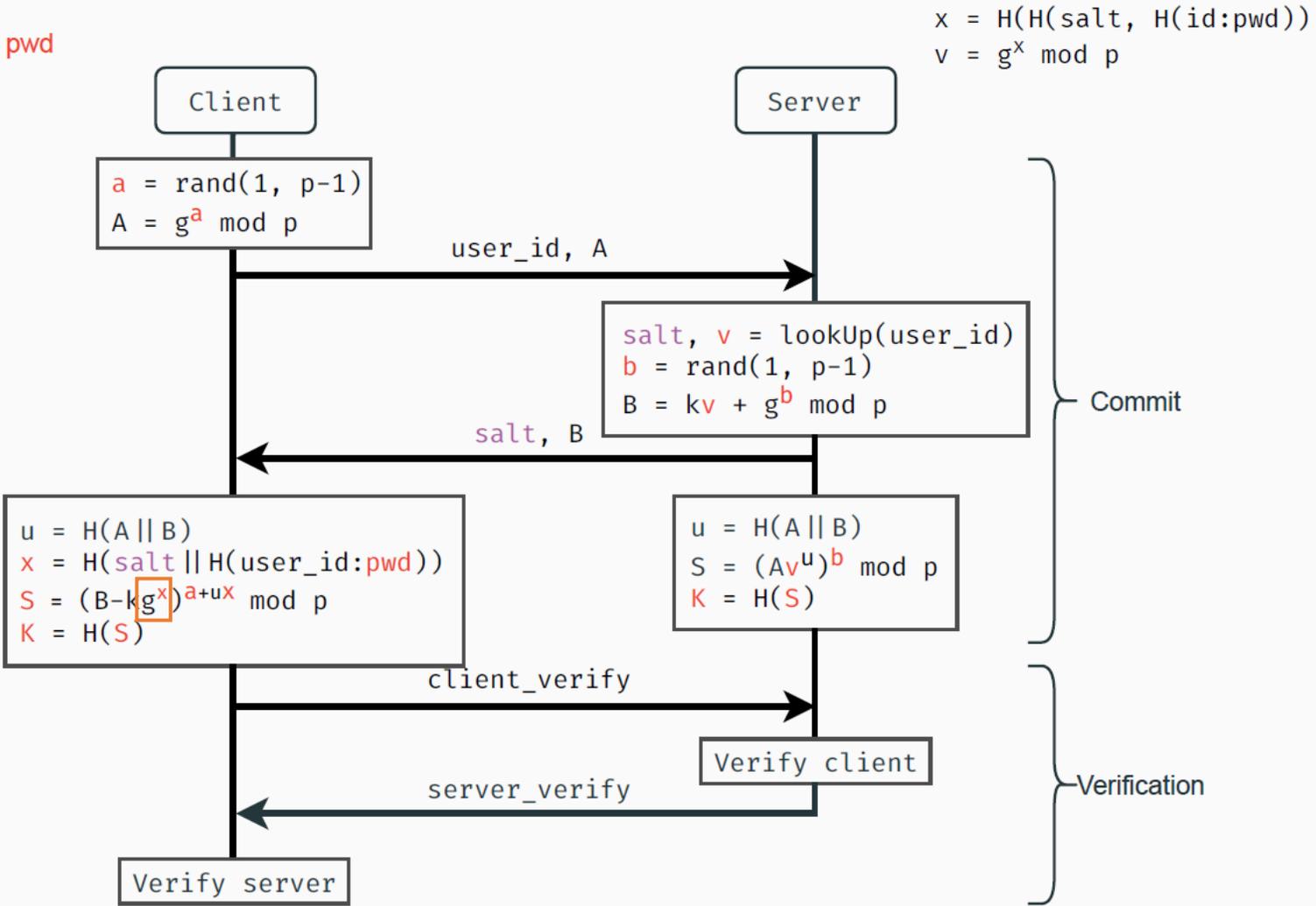


$x = H(H(\text{salt}, H(\text{id}:\text{pwd})))$   
 $v = g^x \text{ mod } p$

Commit

Verification

# SRP Protocol Overview



# Contributions

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1. Study of various SRP implementations
2. Highlight a leakage in the root library used for big number arithmetic (OpenSSL)
3. Design PoCs of an offline dictionary attack recovering the password on impacted projects
4. Outline the importance of SCA, especially for PAKEs

A **cache-attack** that lets us extract information  
during OpenSSL **modular exponentiation**  
allowing to **recover the password** in a **single measure**.

# Our Main Result

Flush+Reload<sup>1</sup> and PDA<sup>2</sup>

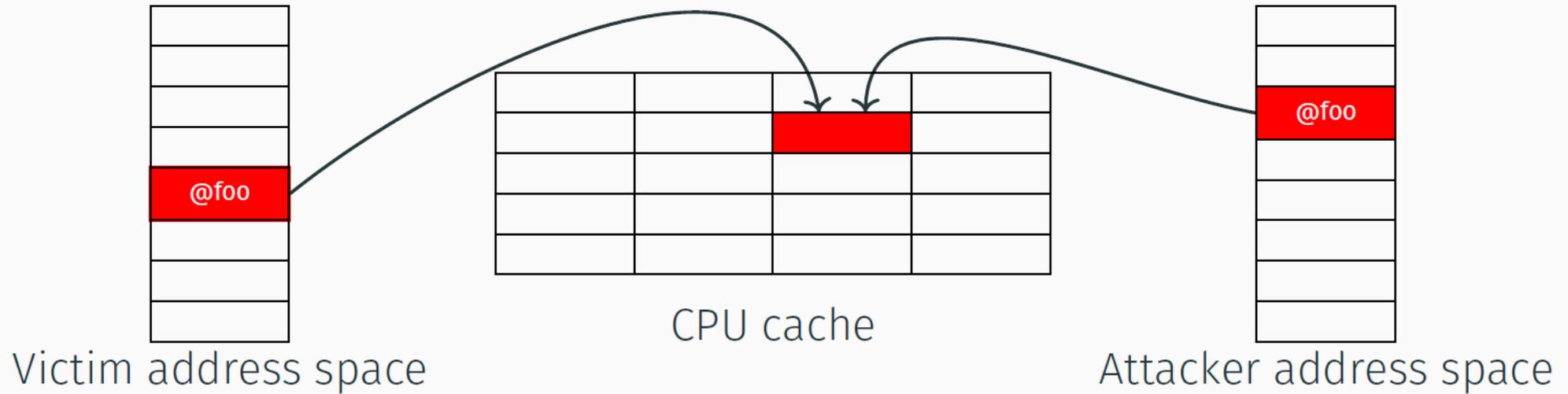
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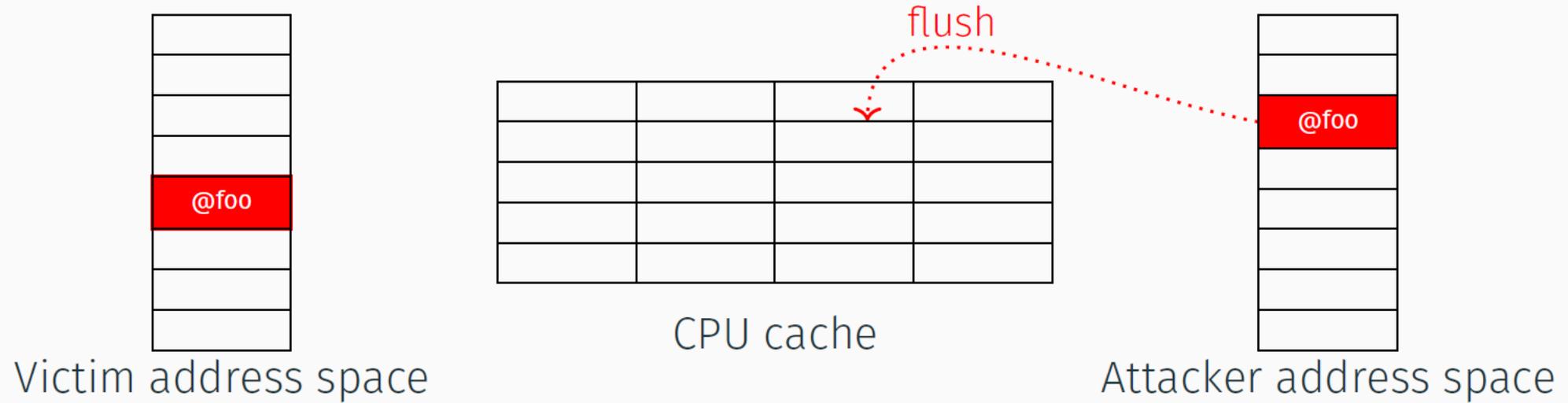
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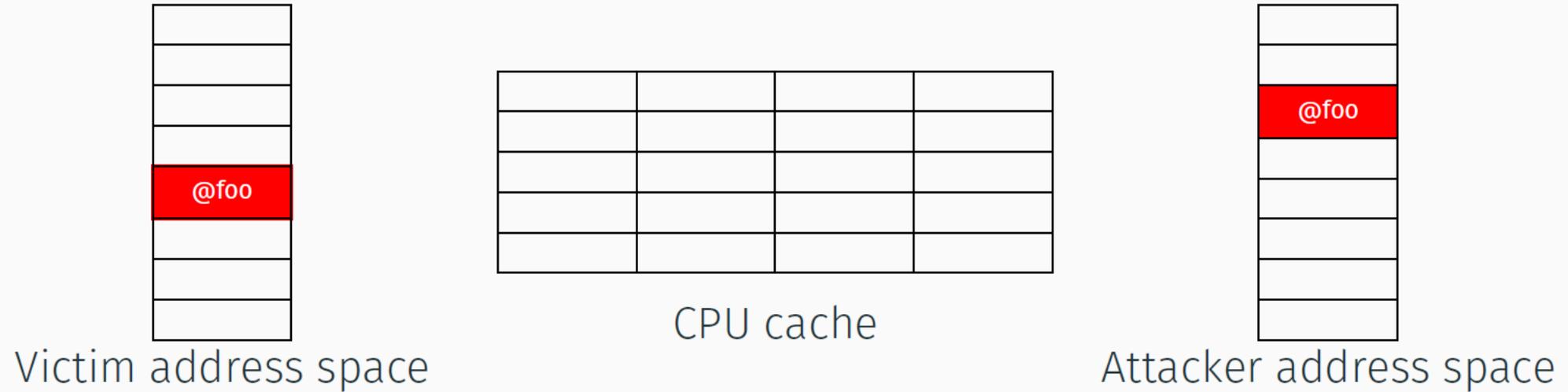
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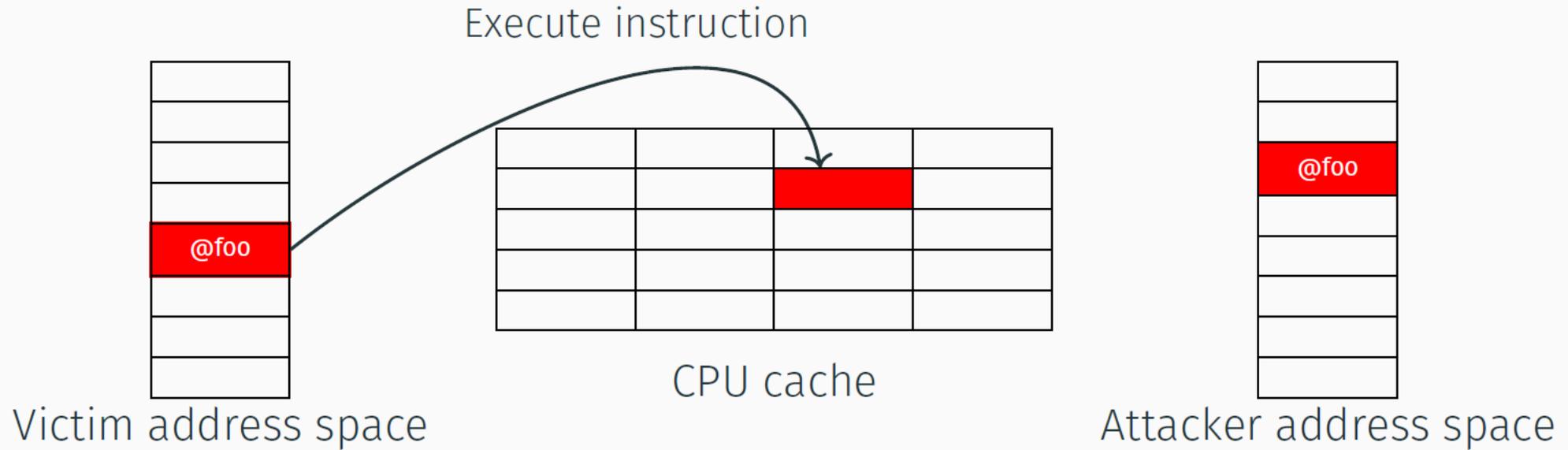
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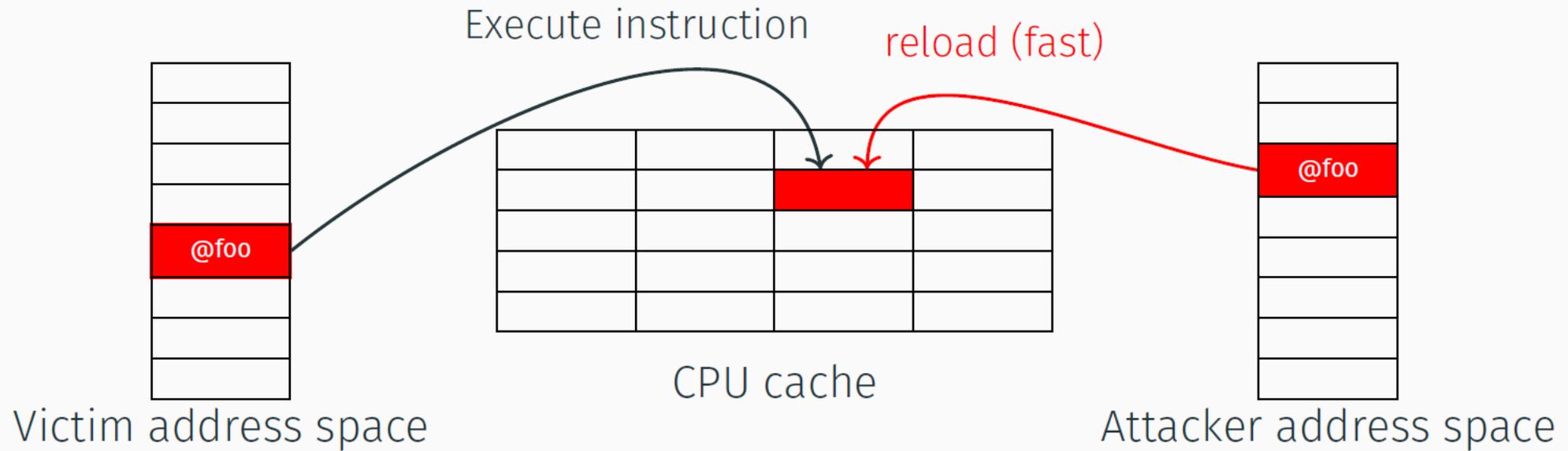
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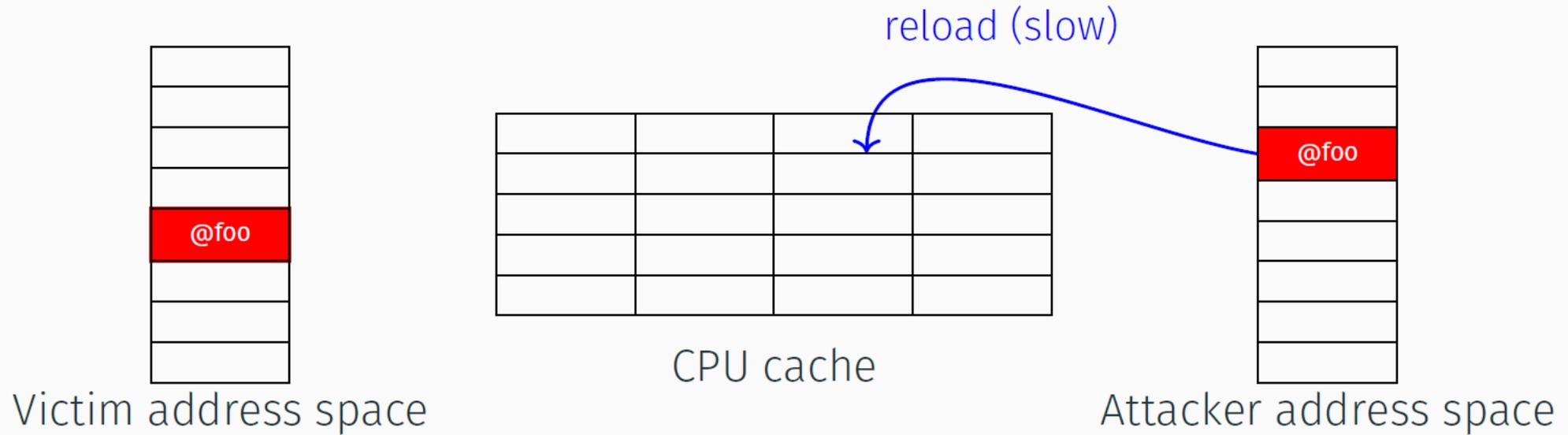
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# FLUSH+RELOAD<sup>1</sup>



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2. Flush the instruction we monitor
3. See how much time it takes to reload
  - Fast  $\Rightarrow$  the victim already executed
  - Slow  $\Rightarrow$  the victim did not

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Flush+Reload<sup>1</sup> and PDA<sup>2</sup>

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Passive offline attack

No error and enough information

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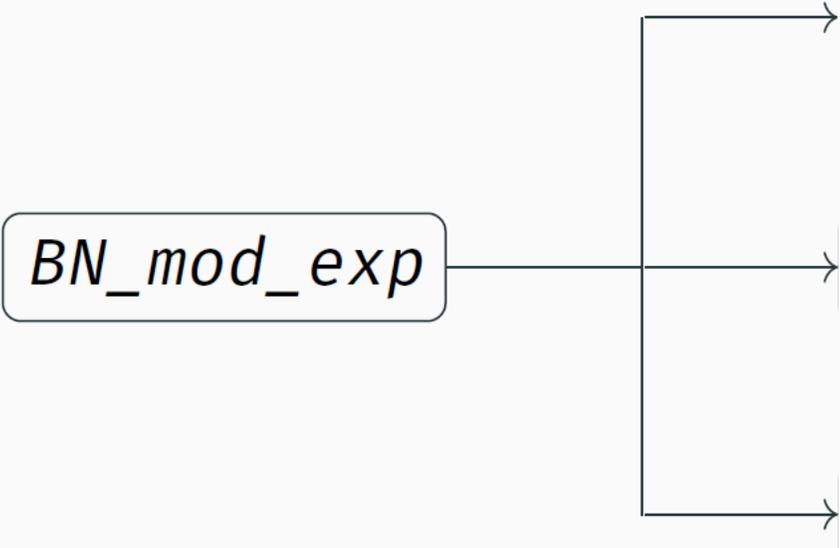
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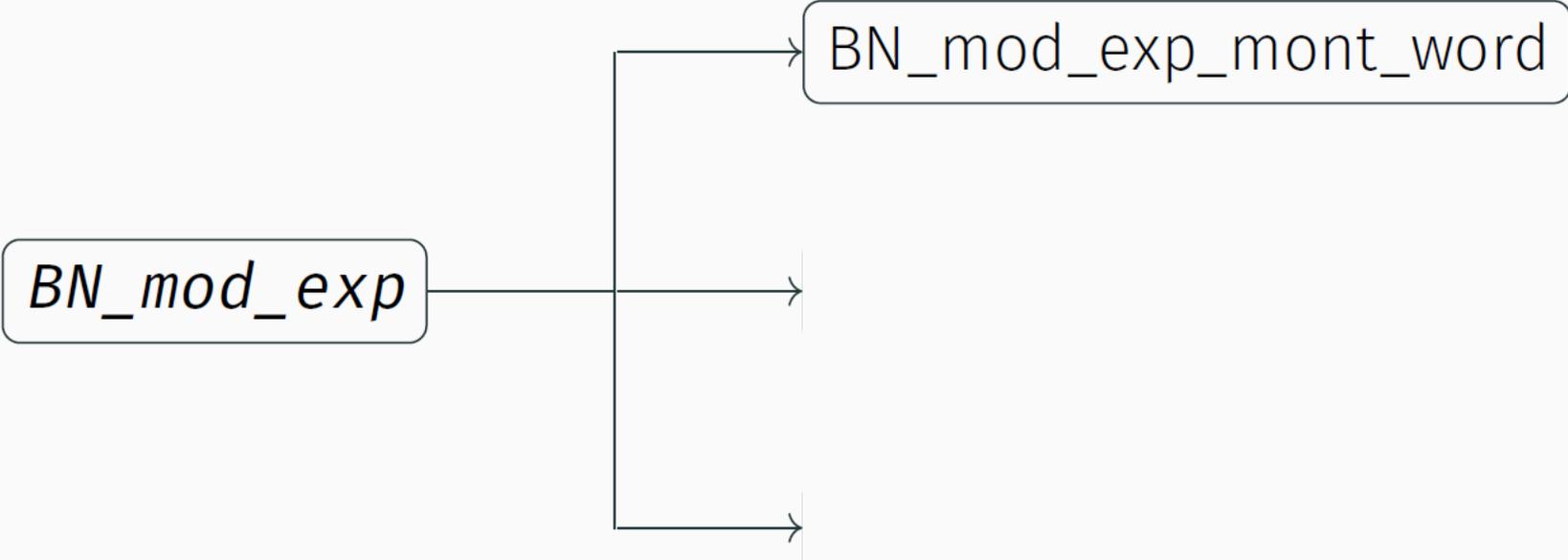
# Modular exponentiation in OpenSSL

*BN\_mod\_exp*

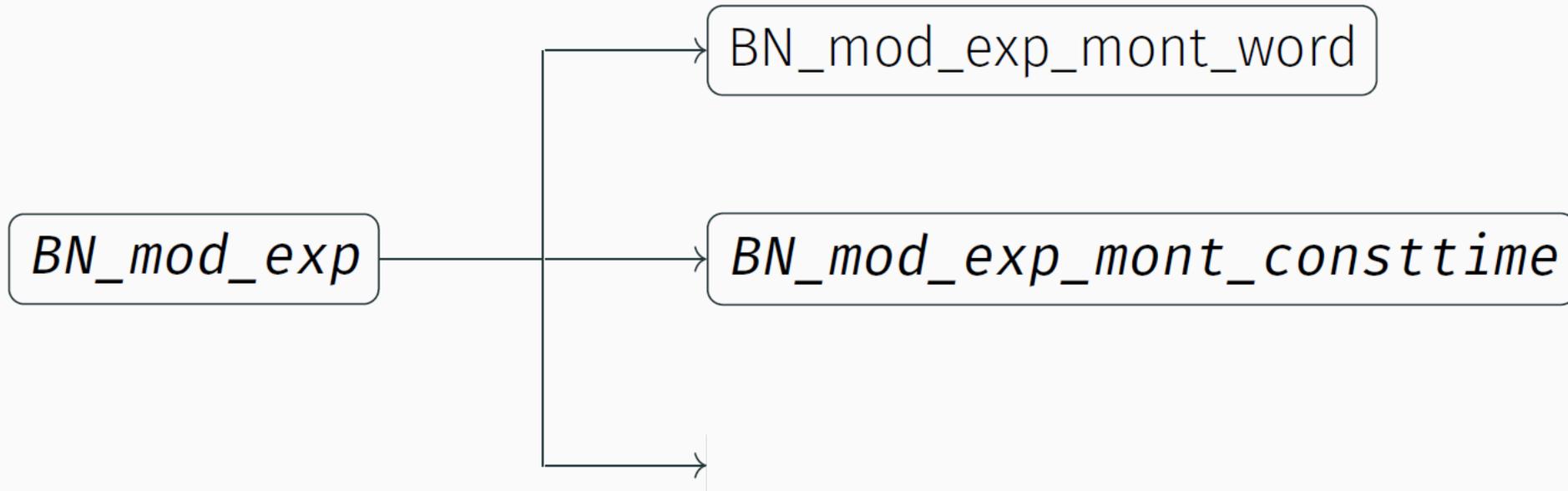
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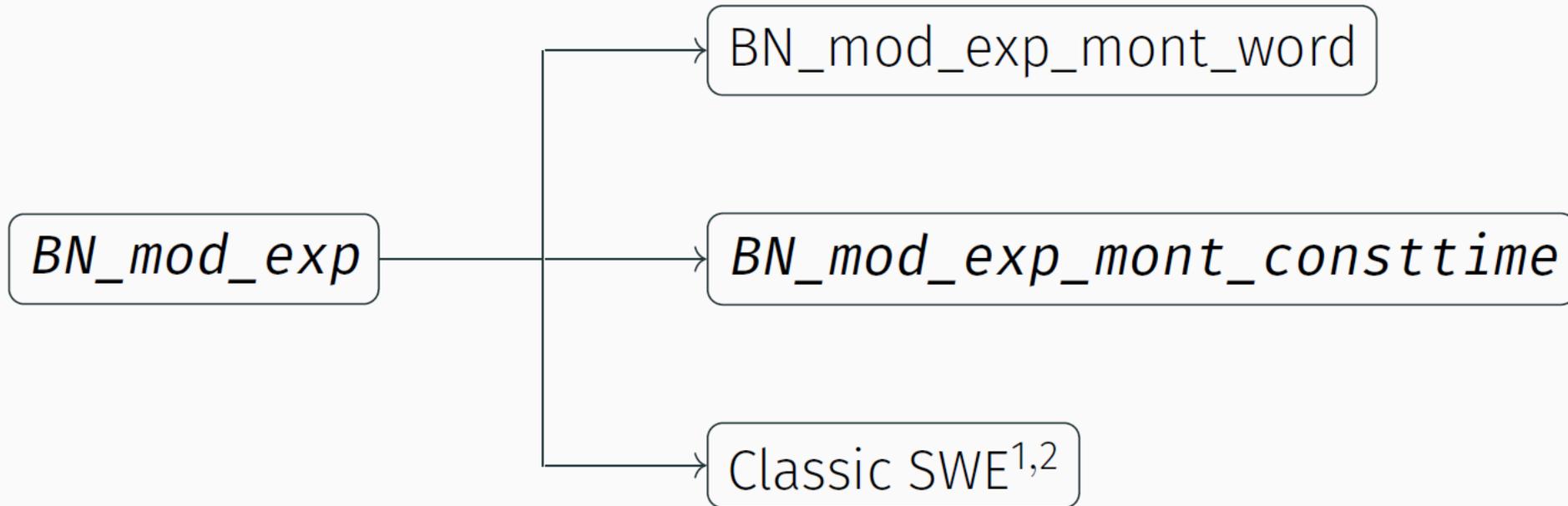
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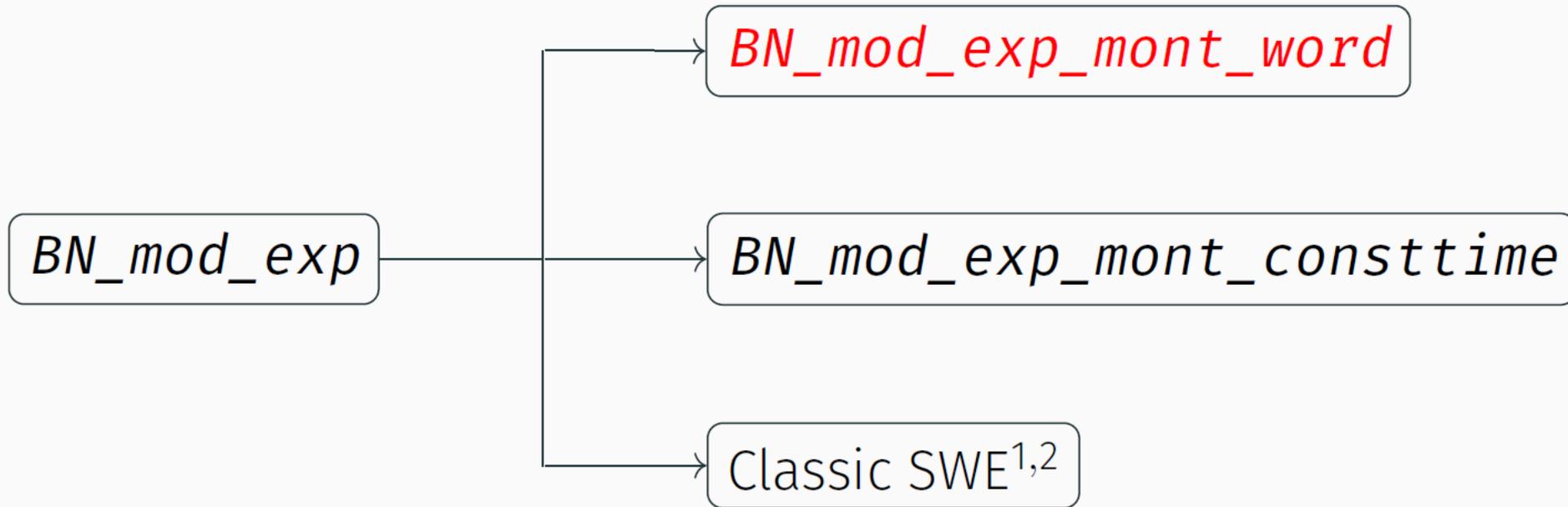
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# Optimized Square-and-Multiply

$$\text{bin}(e) = 1\ 1\ 0\ 1\ 0\ \dots$$

$$\text{res} = g^e \bmod p$$

$w$  is a processor word (e.g. 64 bits)

```
def BN_mod_exp_mont_word(g, w, p):
    ...
    w = g # uint64_t
    res = BN_to_mont_word(w) # bigum
    for b in range(bitlen-2, 0, -1):
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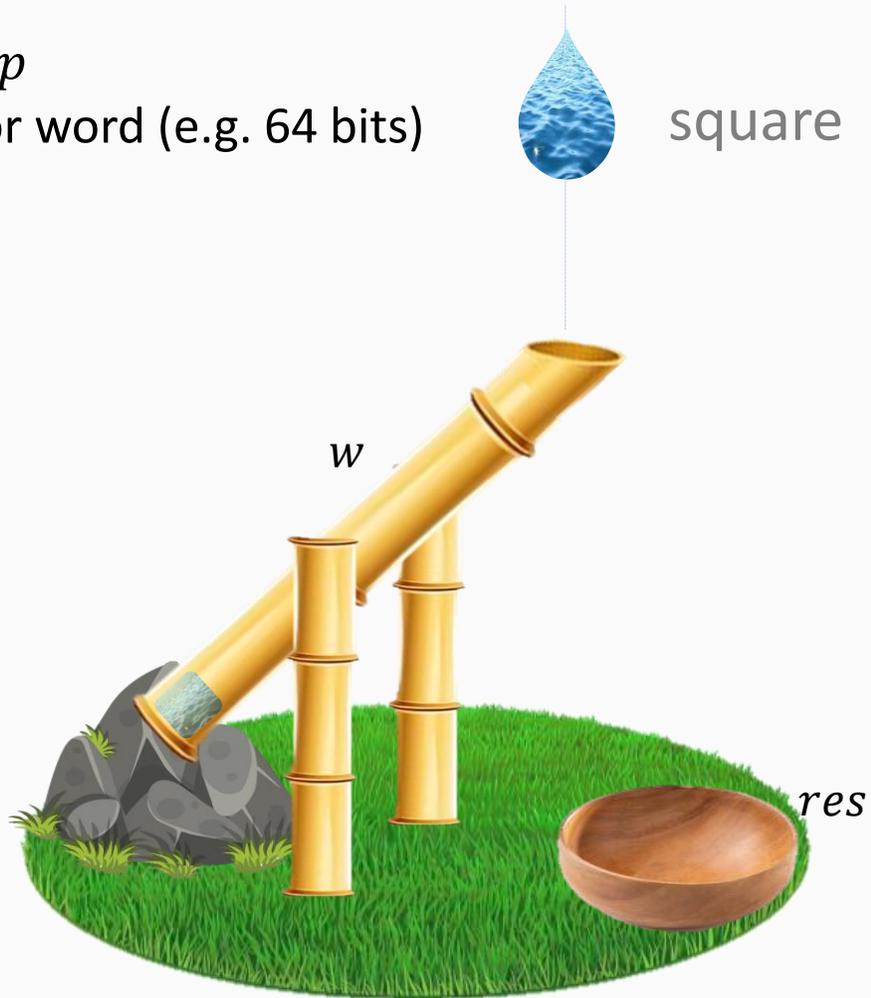
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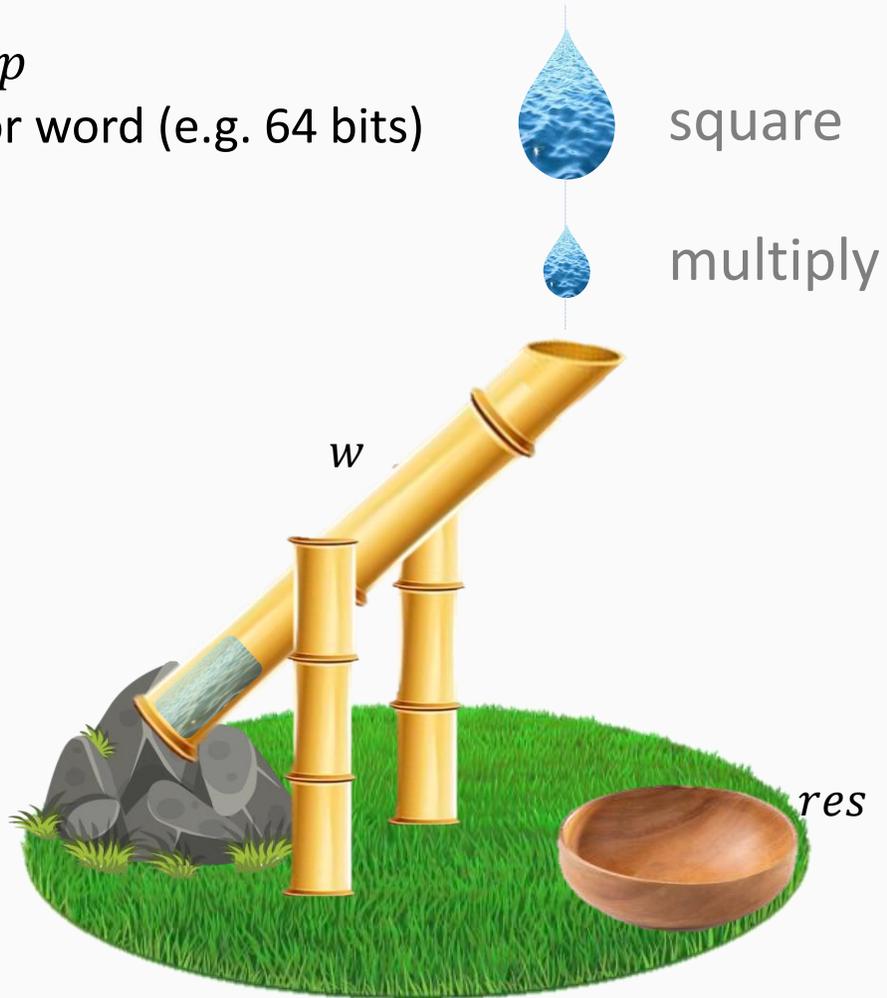
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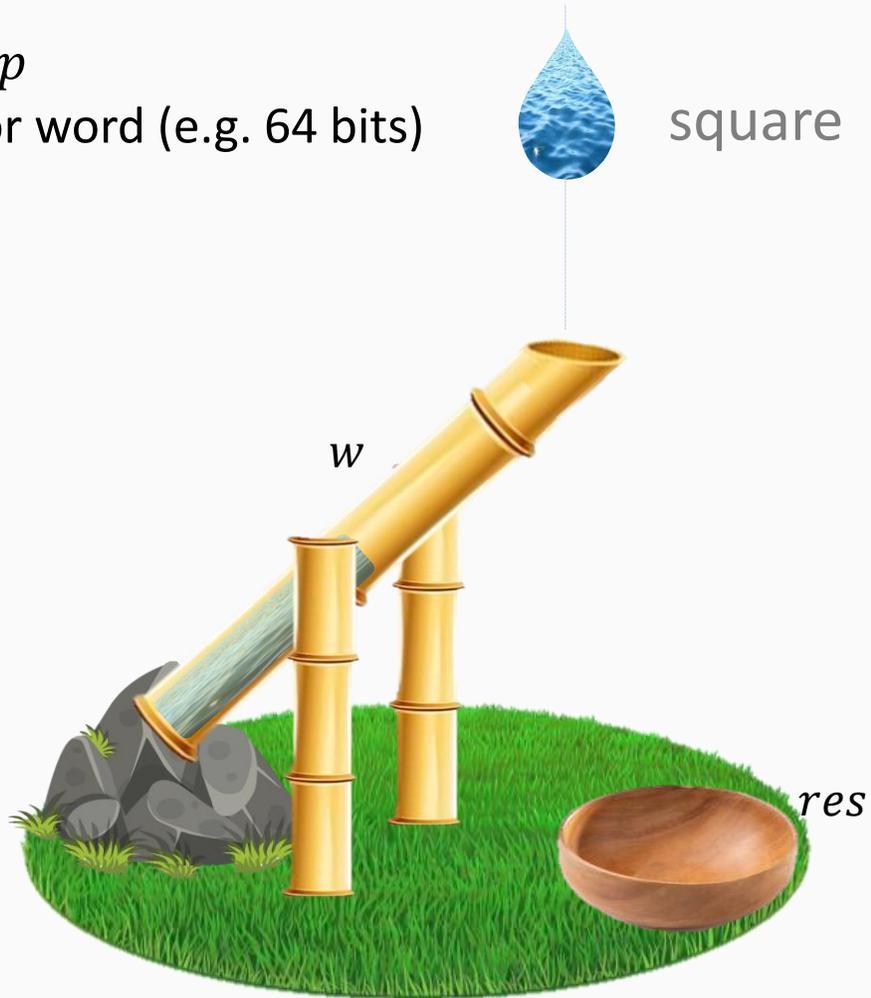
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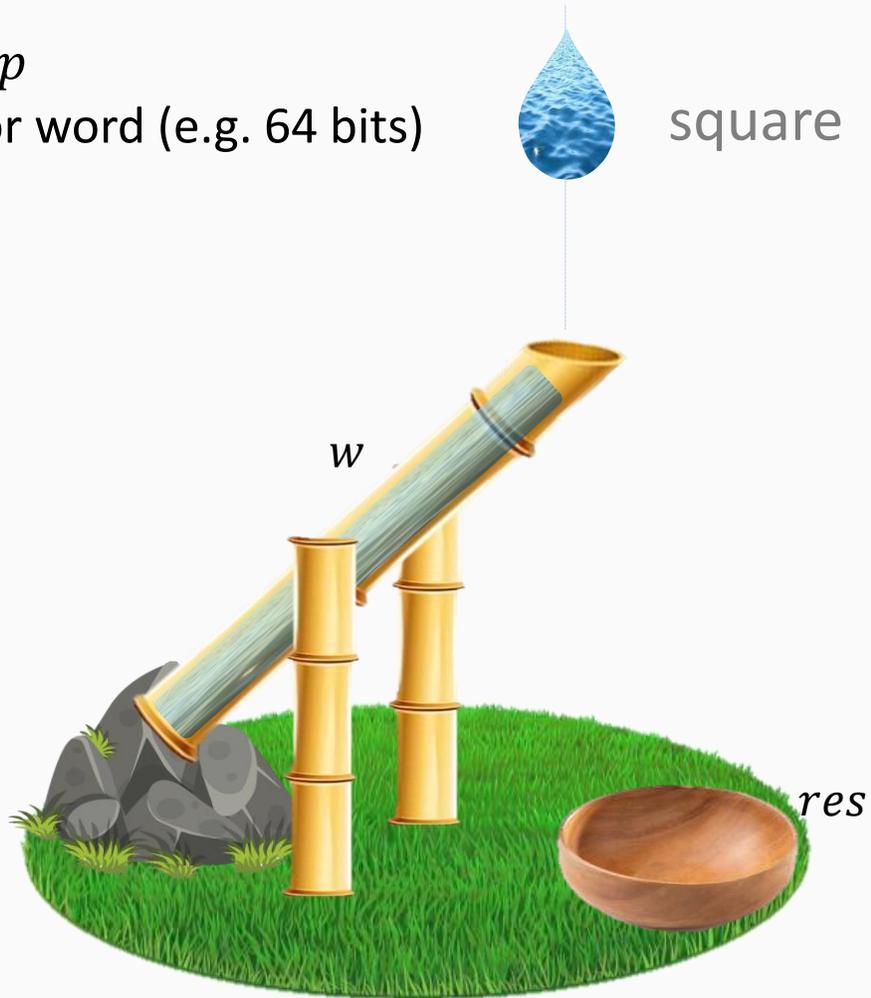
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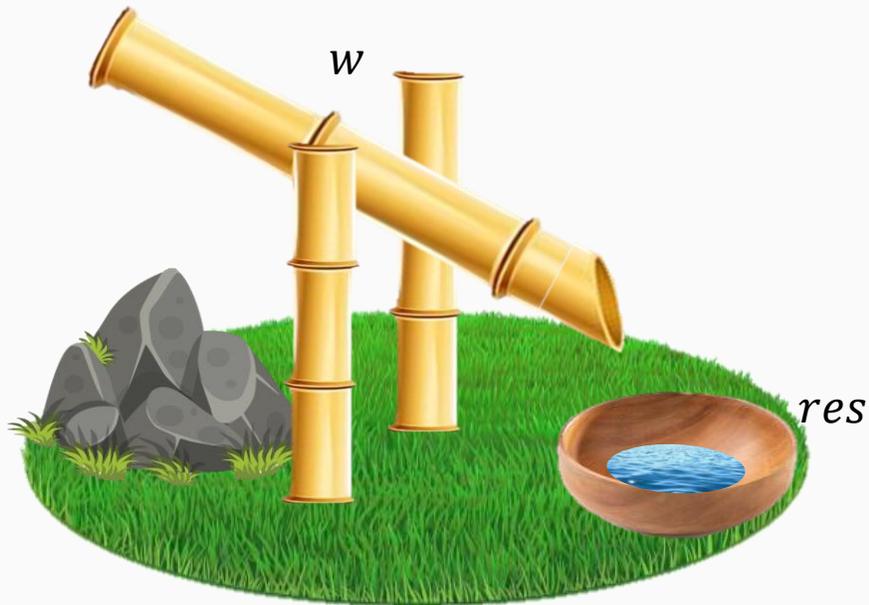
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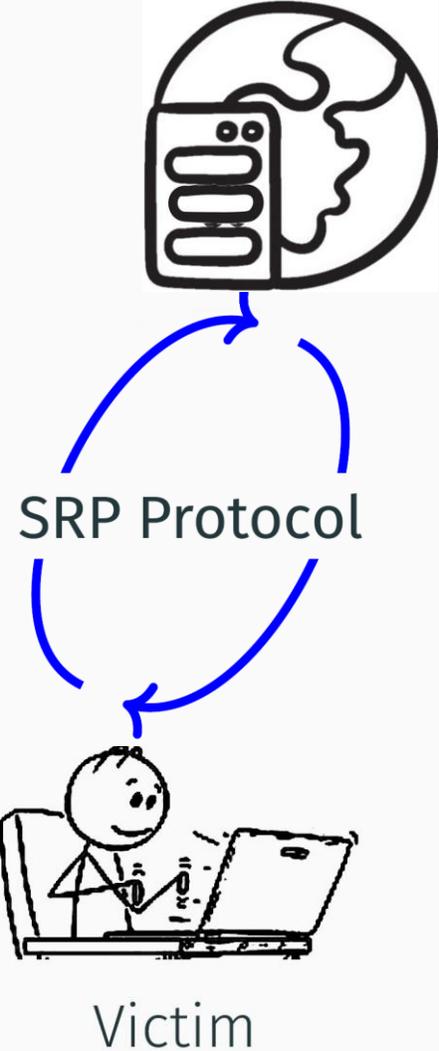
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# Exploiting the Leakage

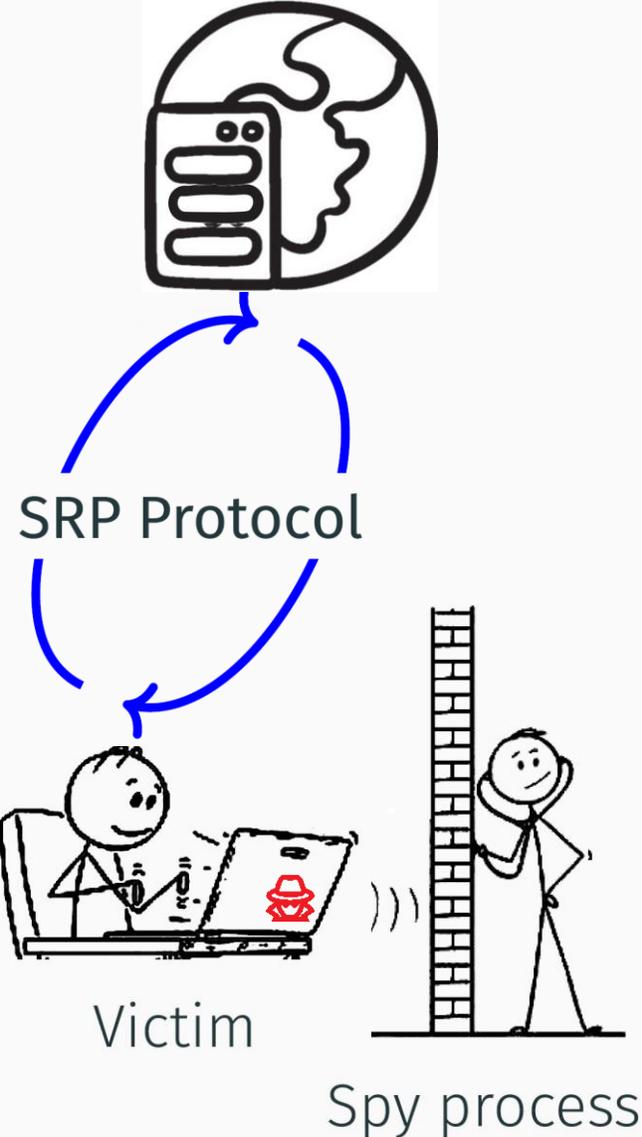
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- Unprivileged spyware on the victim station
- Victim tries to connect
- MitM can help to gather more information (optional)

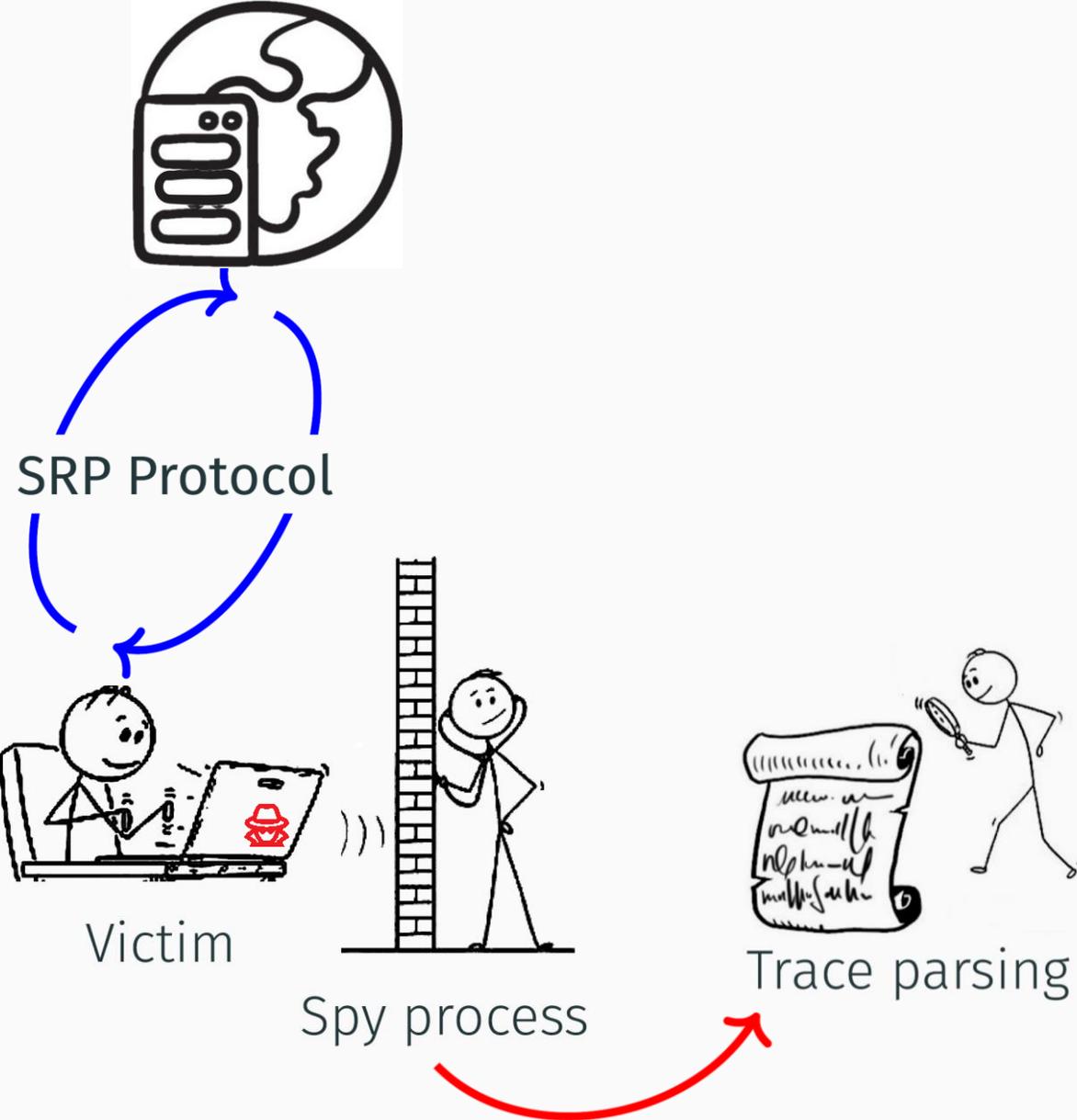
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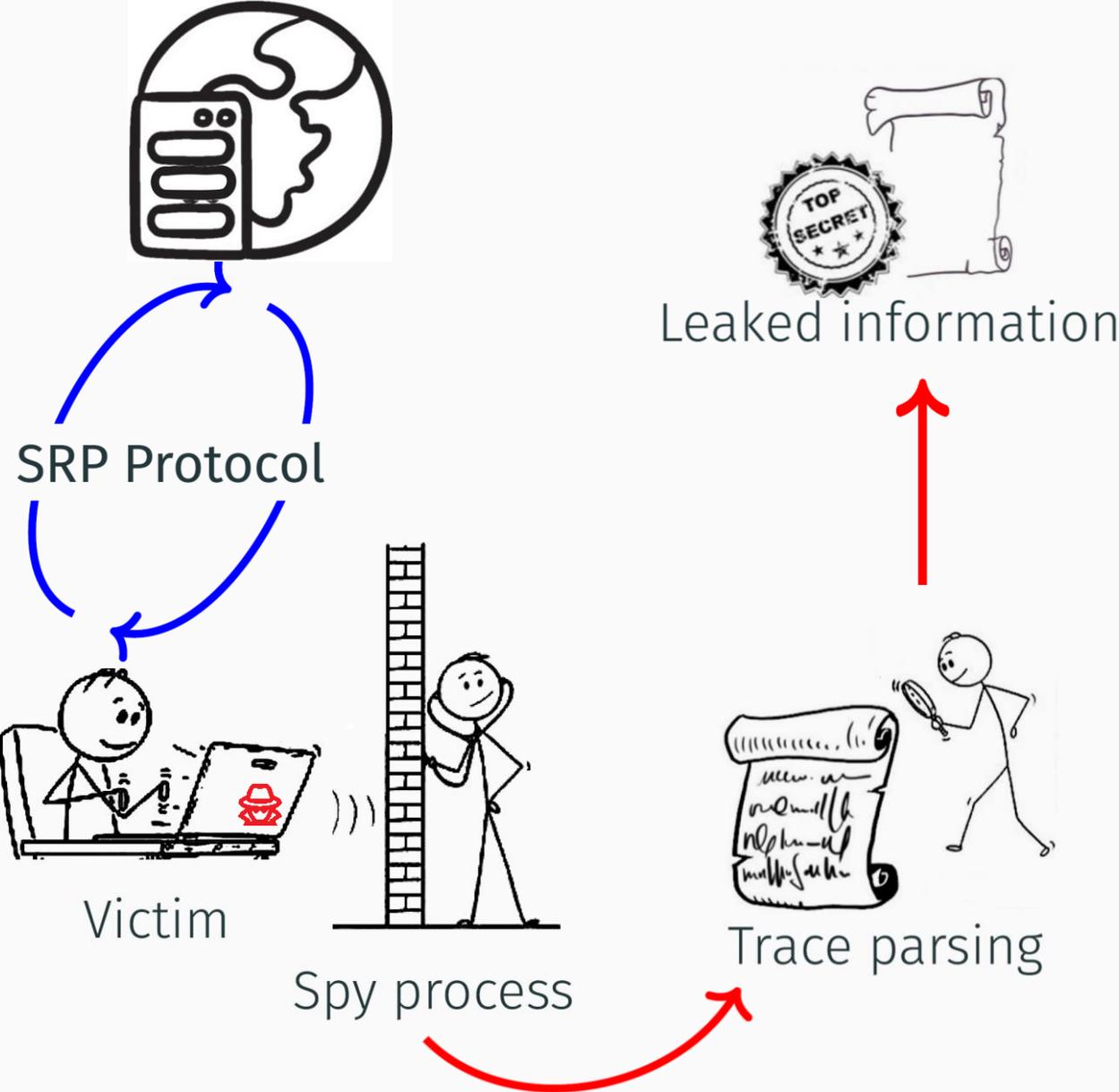
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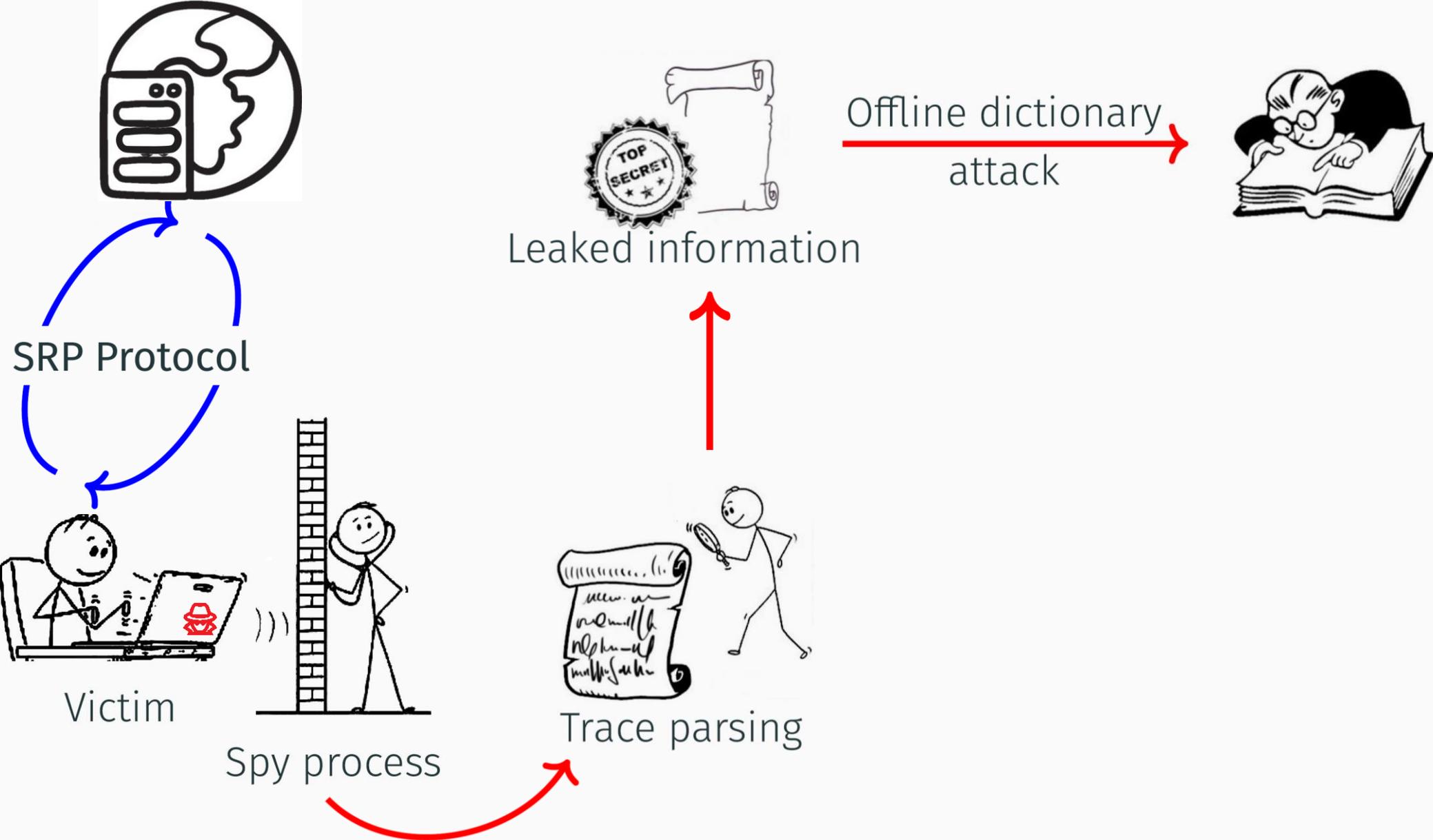
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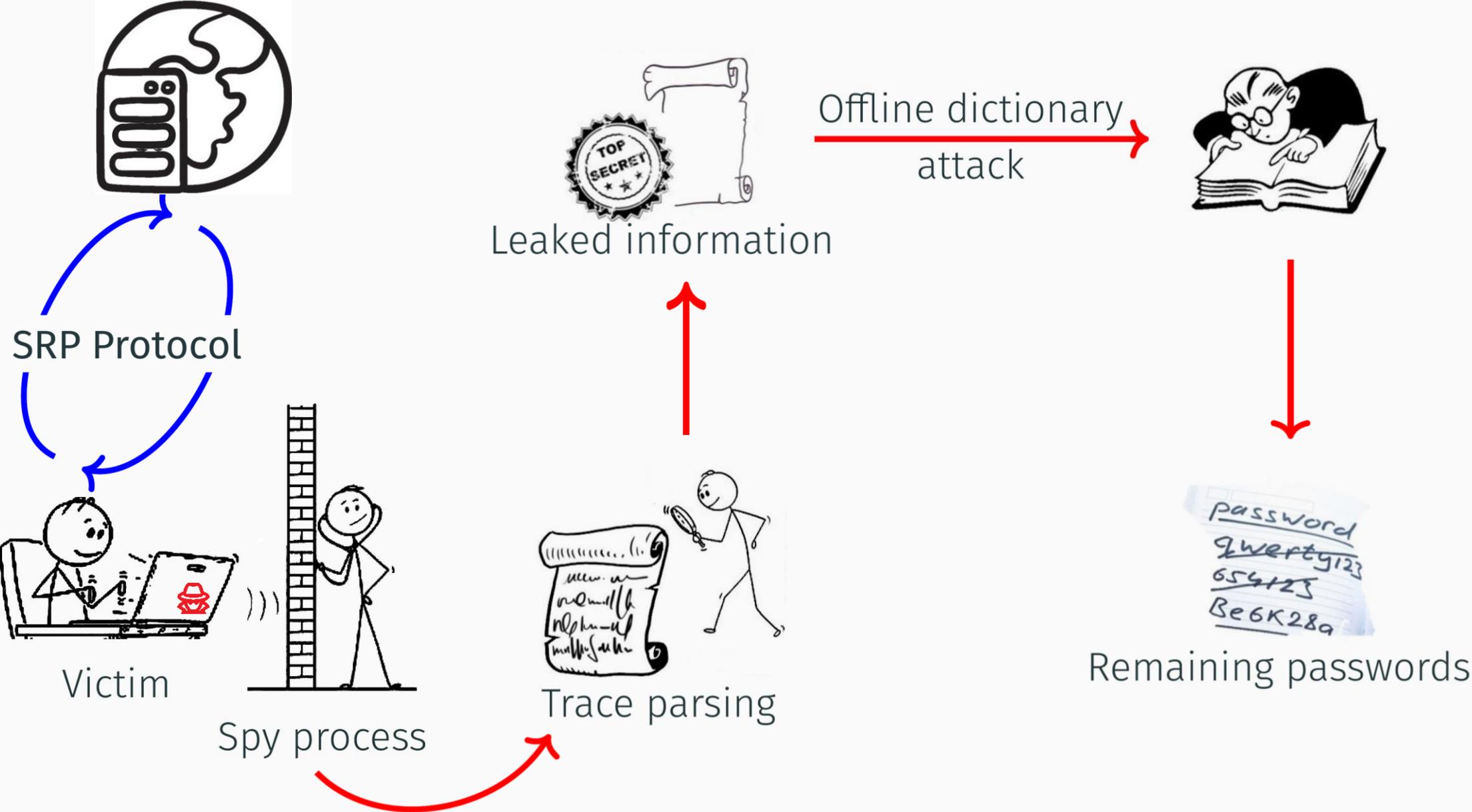
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```

# Trace Acquisition

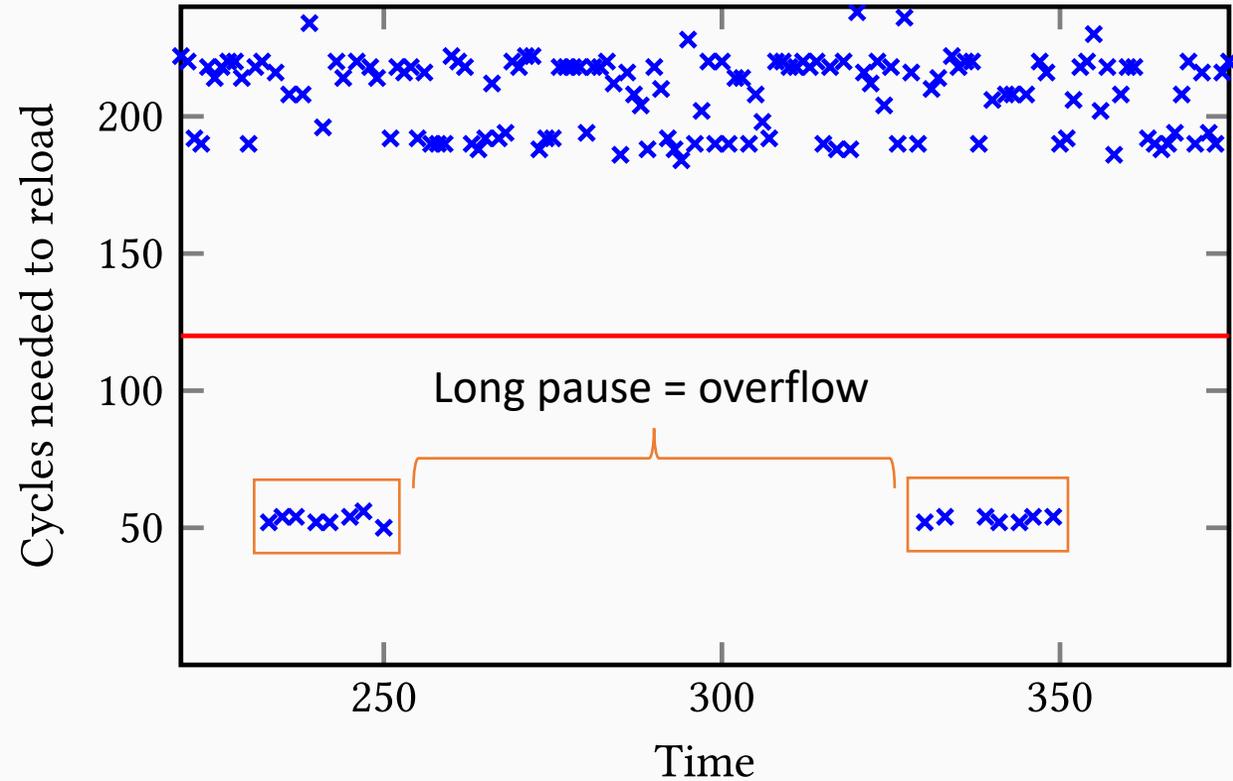
```
def BN_mod_exp_mont_word(g, w, p):  
    ...  
    w = g # uint64_t  
    res = BN_to_mont_word(w) # bigum  
    for b in range(bitlen-2, 0, -1):  
        next_w = w x w  
        if next_w/w != w:  
            res = BN_mod_mul(res, w, p)  
            next_w = 1  
        w = next_w  
     → res = BN_sqr(res)  
    if BN_is_bit_set(x, b):  
        next_w = w x g  
        if next_w/g != w:  
            res = BN_mod_mul(res, w, p)  
            next_w = g  
        w = next_w  
    ...
```

# Trace Acquisition

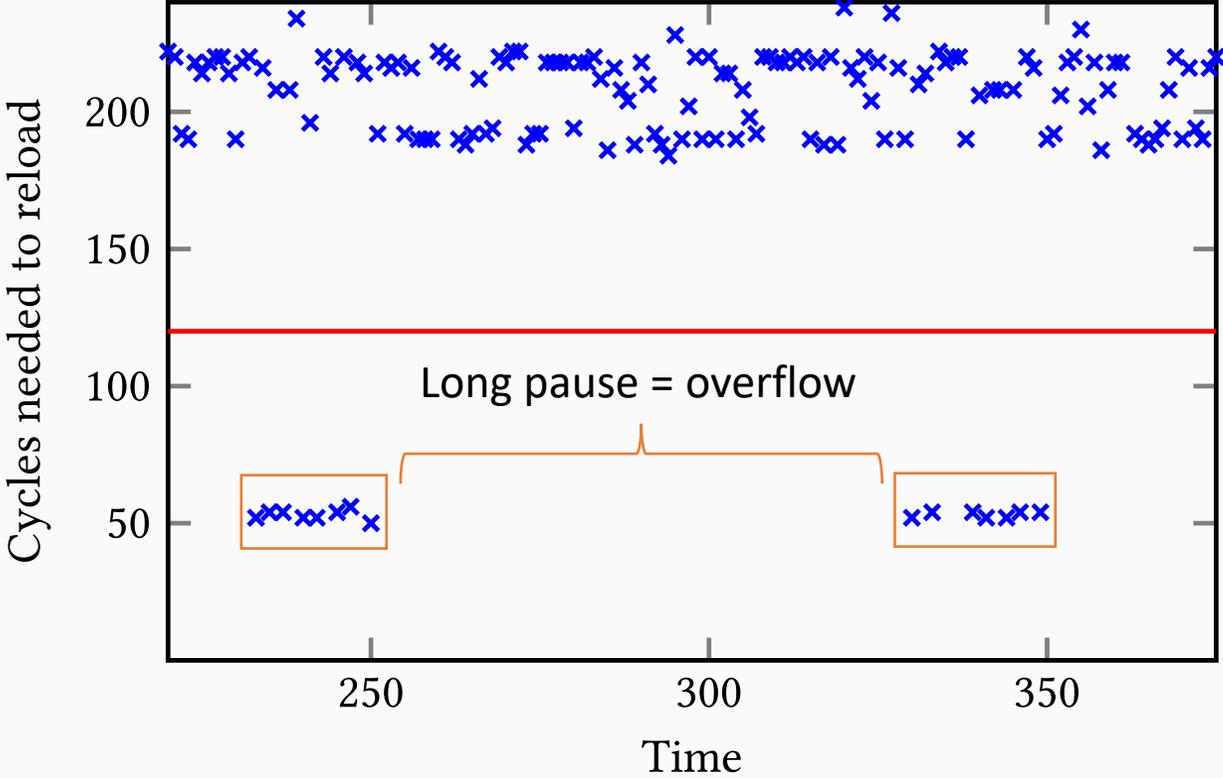
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```

# Trace Acquisition

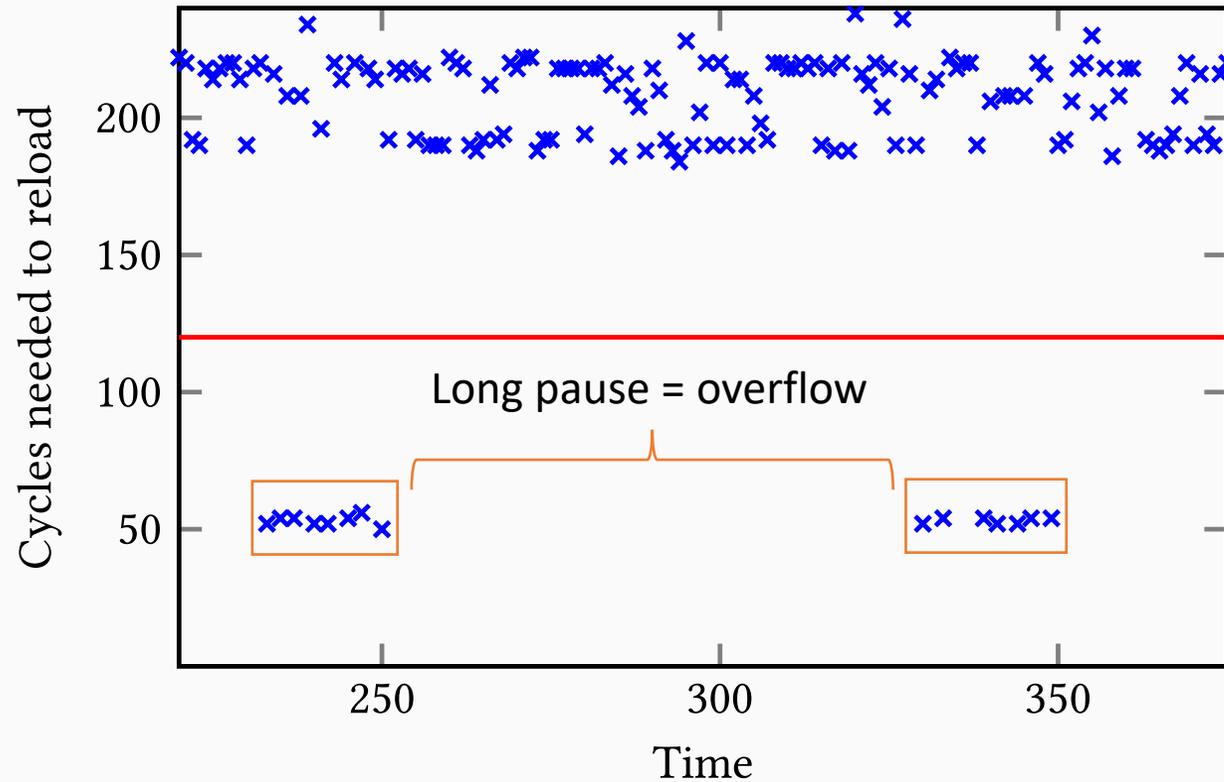
```
def BN_mod_exp_mot_word(g, w, p):  
    ...  
    w = g # uint64_t  
    res = BN_to_mont_word(w) # bigum  
    for b in range(bitlen-2, 0, -1):  
        next_w = w x w  
        if next_w/w != w:  
            ↻ → res = BN_mod_mul(res, w, p)  
                next_w = 1  
        w = next_w  
        🕶 → res = BN_sqr(res)  
        if BN_is_bit_set(x, b):  
            next_w = w x g  
            if next_w/g != w:  
                res = BN_mod_mul(res, w, p)  
                next_w = g  
            w = next_w  
    ...
```



# Trace Interpretation



# Trace Interpretation



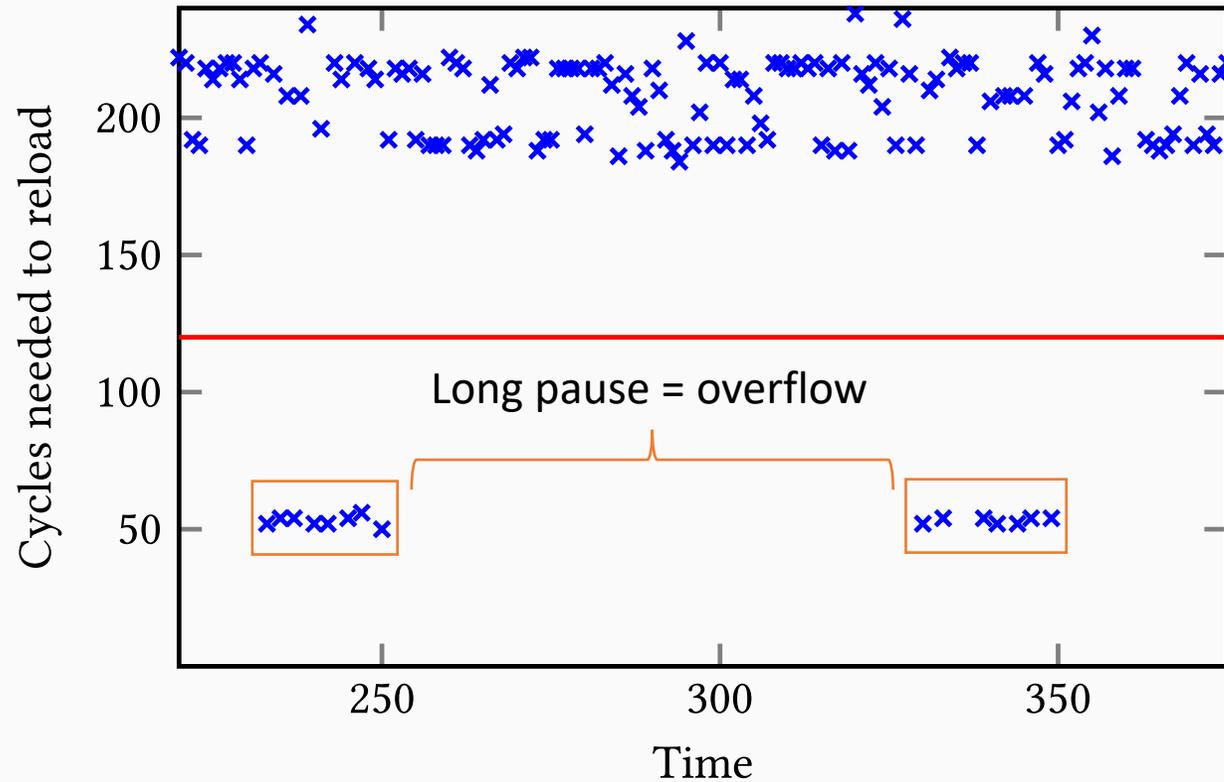
Rules ( $b \in \{0,1\}$ ):

$Vvvv \rightarrow 111b$

$Vvvvv \rightarrow yyyyb, yyyy \in \{110b, 10bb, 0111\}$

$Vv\dots v \rightarrow 0 \dots 0yyyyb$

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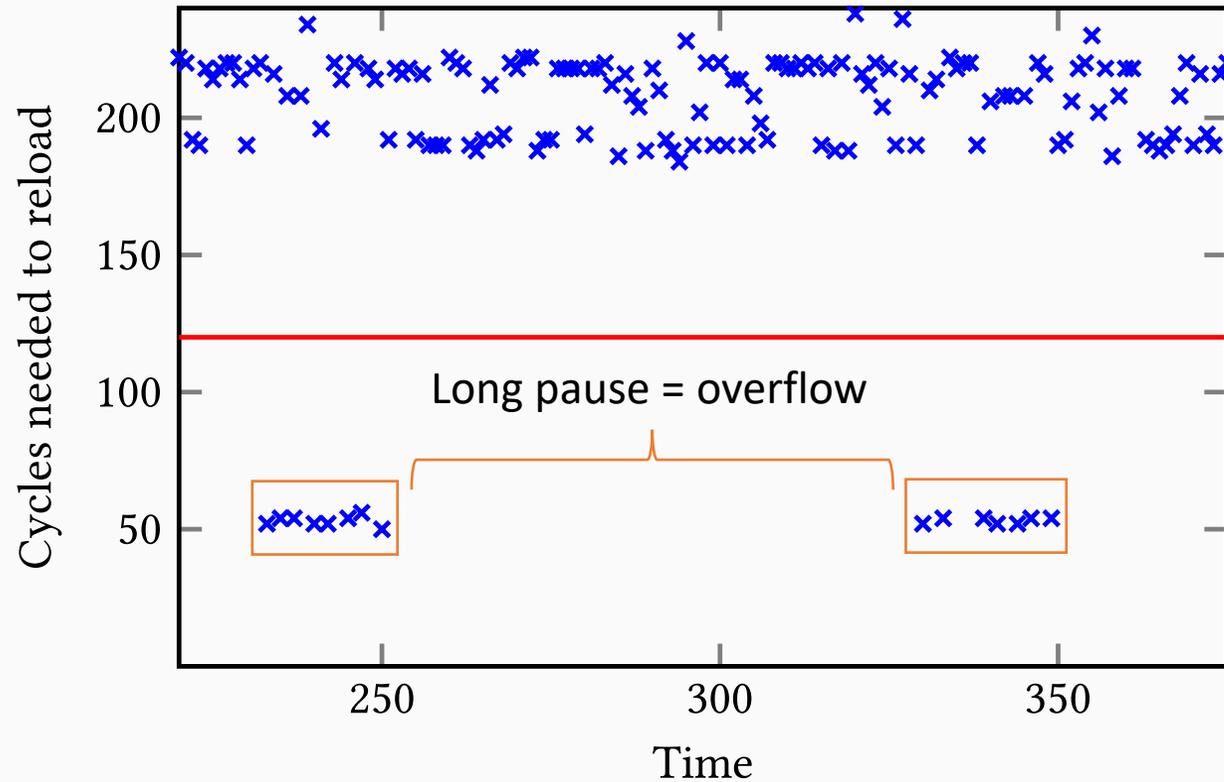
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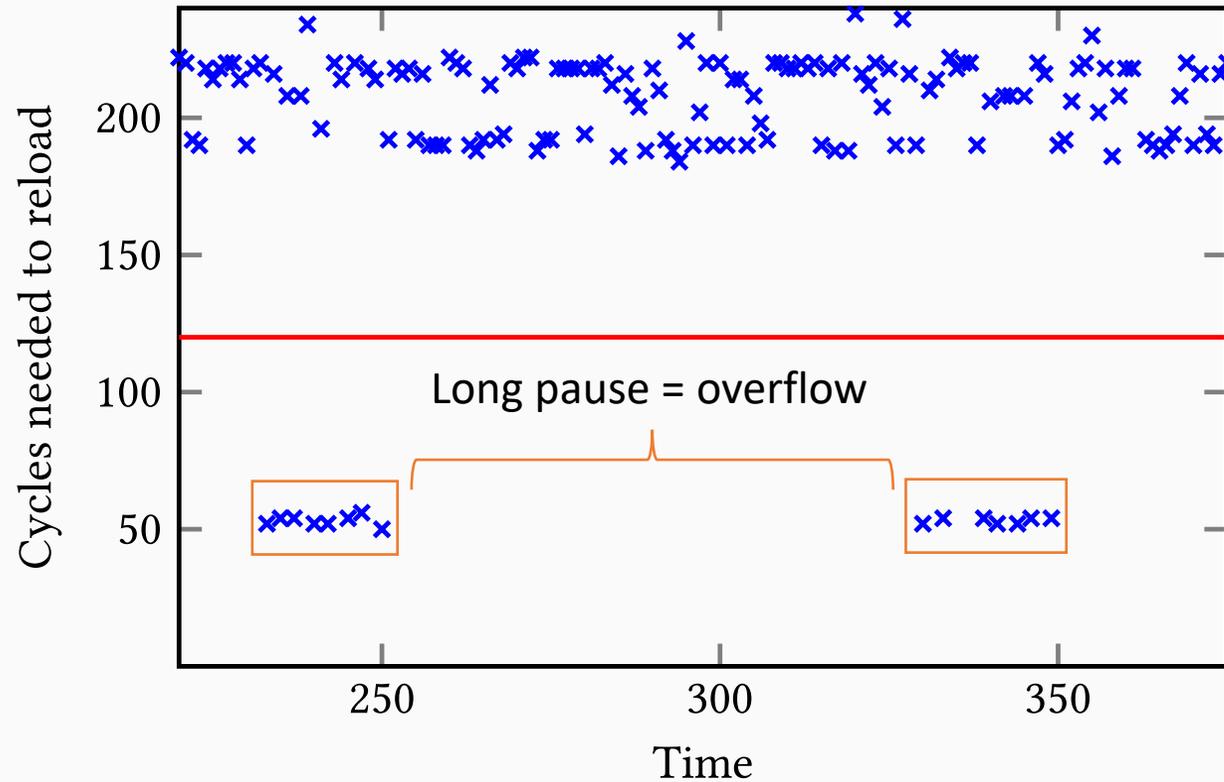
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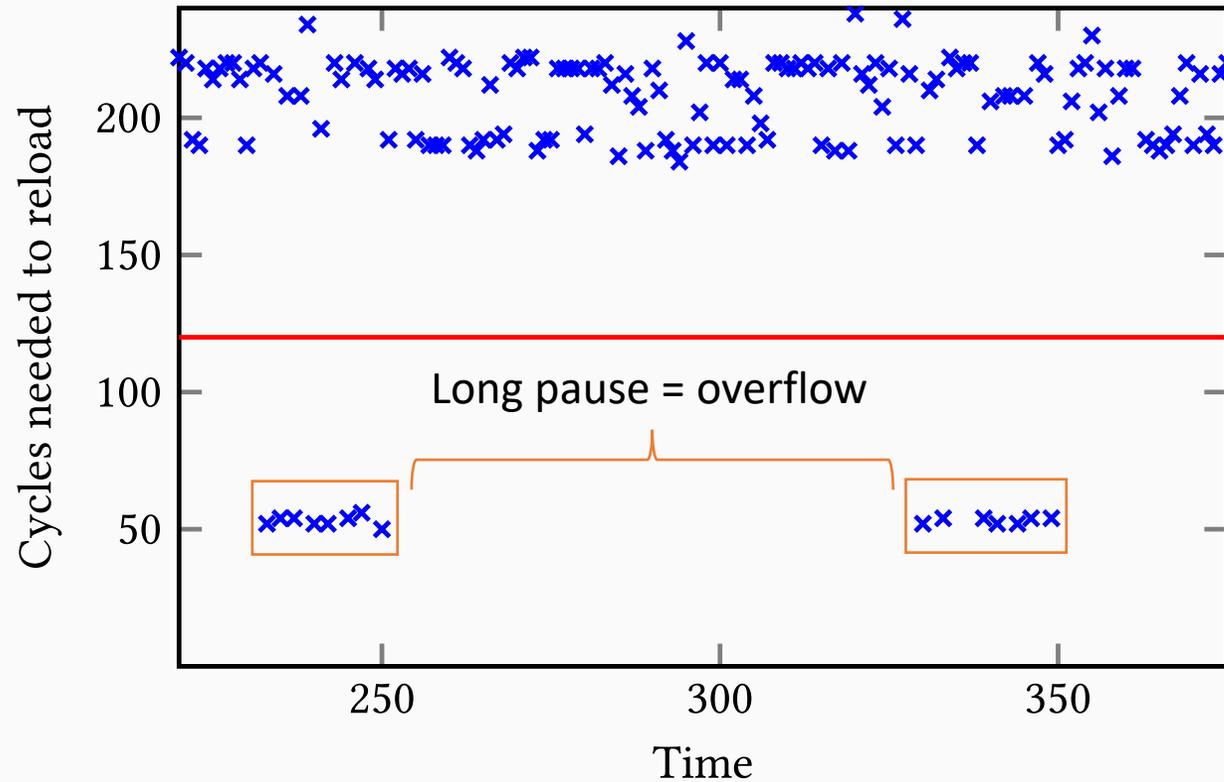
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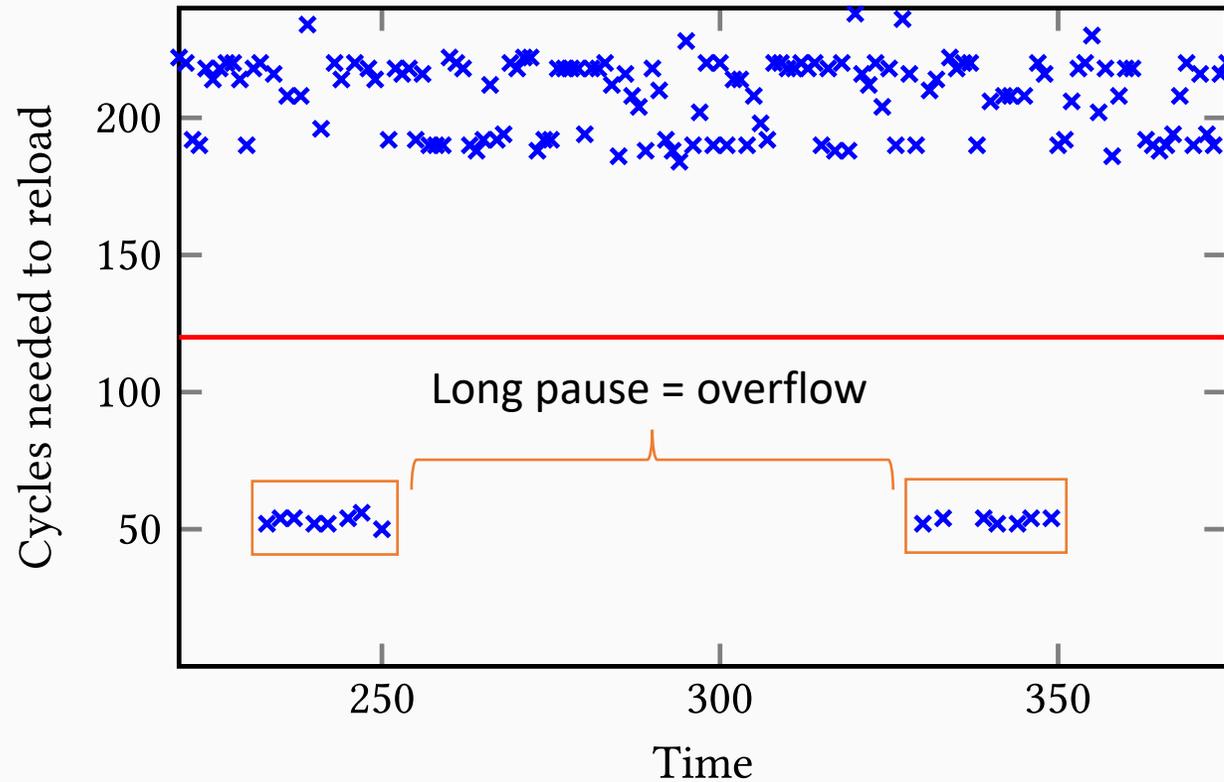
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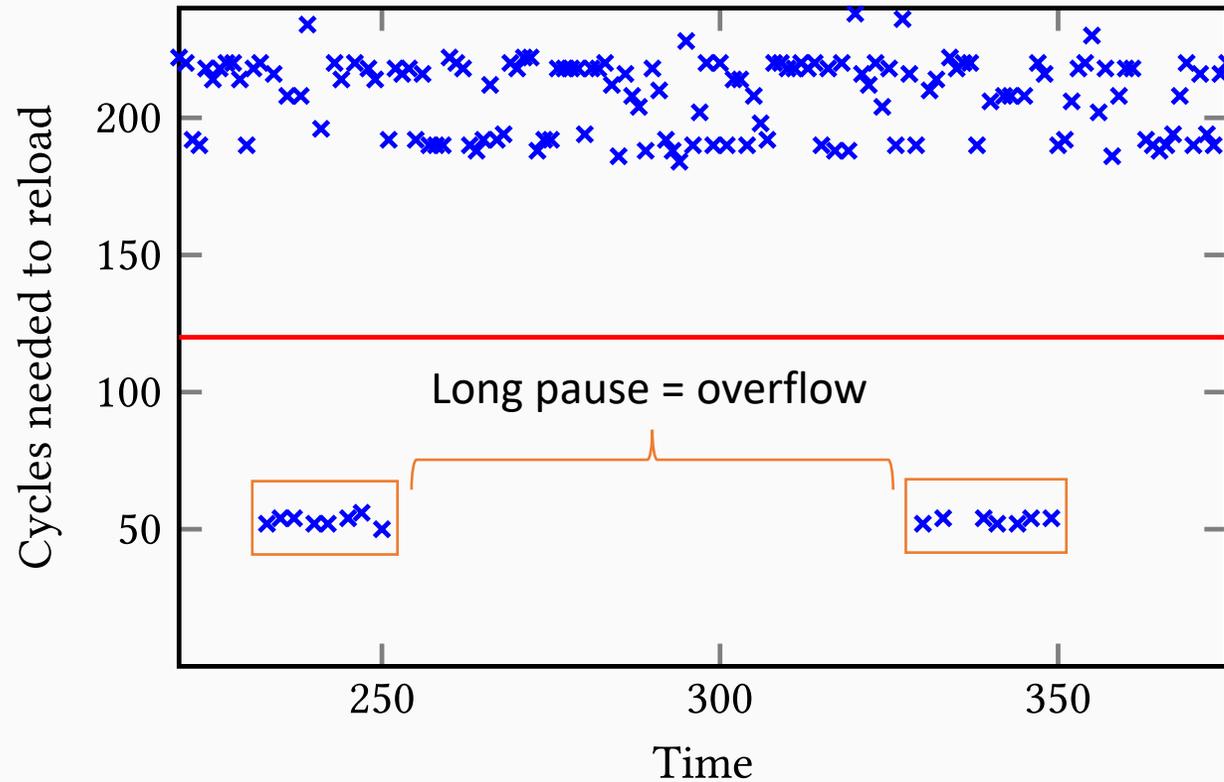
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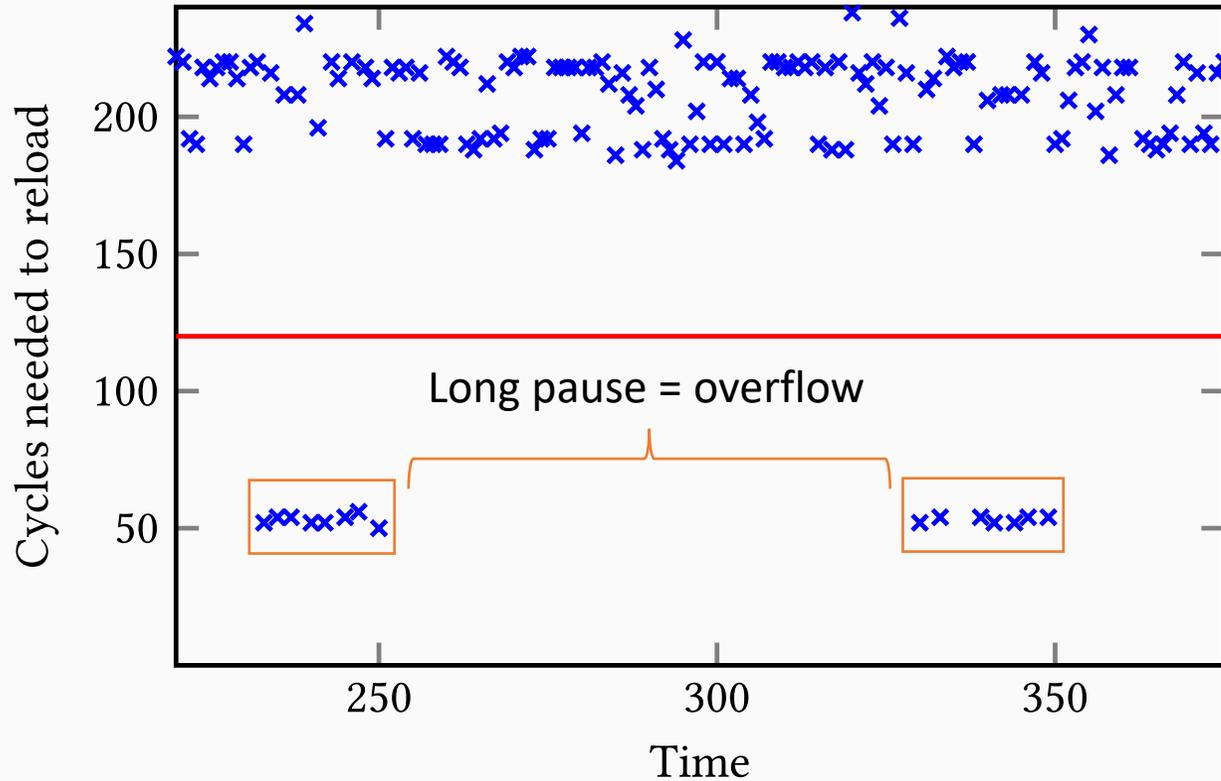
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$Vvvv \ Vvvvv \ Vvvvvv \ Vvvvv \ Vvvvvv \ Vvvvvv \ Vvvv$   
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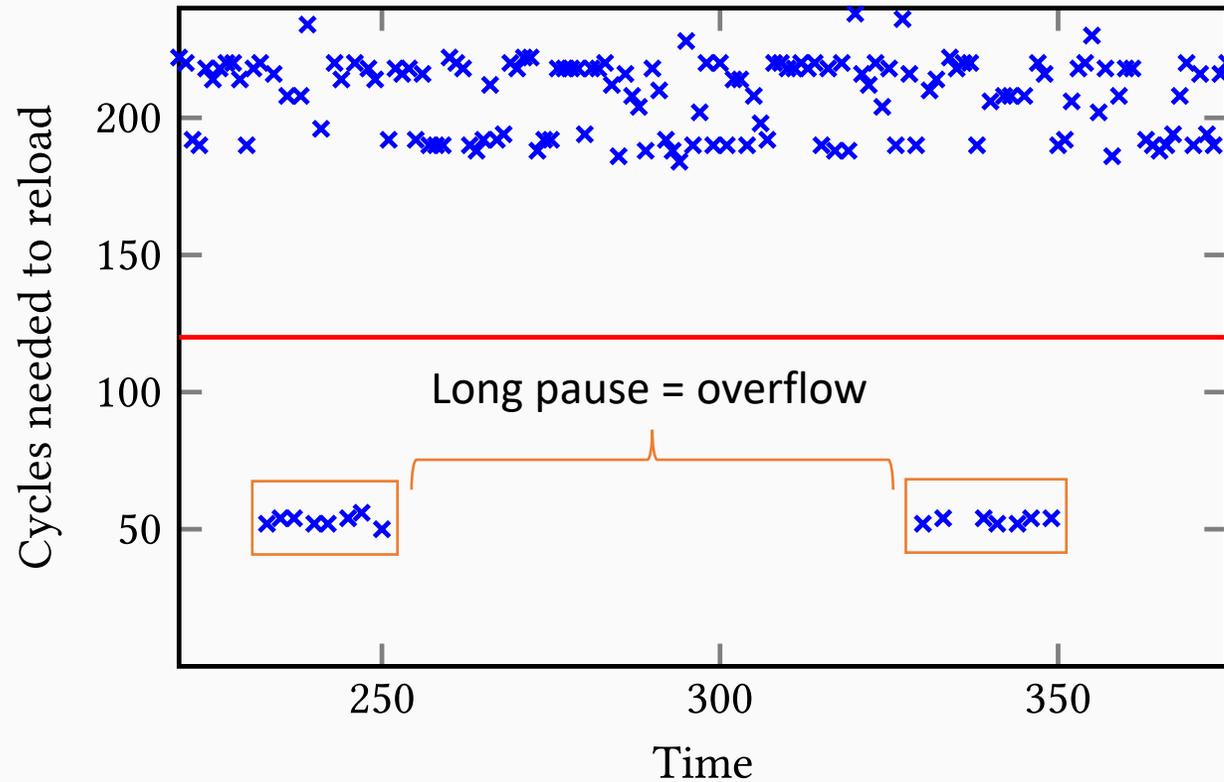
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# Dictionary Attack

Client :  $x = H(\text{salt} \parallel H(\text{user\_id}:\text{password}))$   
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Recovered:            1 1 1 b y y y y b 0 y y y y b 1 1 1 b 0 y y y y b

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Recovered:	1 1 1 b y y y y b 0 y y y y b 1 1 1 b 0 y y y y b
pwd_1	1 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 1
pwd_2	1 1 0 0 1 0 1 1 1 1 1 1 0 0 0 0 0 1 0 1 1 1 0 1
pwd_3	0 1 1 1 0 0 0 0 0 0 0 0 1 0 0 1 0 0 0 0 1 1 0 0 0
pwd_4	1 1 1 1 1 1 0 0 0 0 1 0 1 1 0 1 1 1 0 0 0 1 1 1 1
pwd_5	0 1 1 1 1 0 1 1 1 1 0 0 1 0 1 1 1 0 0 0 0 1 0 0 0
...	
pwd_n	1 0 0 0 1 1 0 0 0 0 0 0 0 0 0 1 1 0 1 1 0 0 1 0 1

---

Password	X value
----------	---------

---

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Recovered:            1 1 1 b y y y y b 0 y y y y b 1 1 1 b 0 y y y y b

pwd\_1                1 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 1

pwd\_2                1 1 0 0 1 0 1 1 1 1 1 1 0 0 0 0 1 0 1 1 1 0 1

pwd\_3                0 1 1 1 0 0 0 0 0 0 0 0 1 0 0 1 0 0 0 0 1 1 0 0 0

pwd\_4                1 1 1 1 1 1 0 0 0 0 1 0 1 1 0 1 1 1 0 0 0 1 1 1 1

pwd\_5                0 1 1 1 1 0 1 1 1 1 0 0 1 0 1 1 1 0 0 0 0 1 0 0 0

...

pwd\_n                1 0 0 0 1 1 0 0 0 0 0 0 0 0 0 1 1 0 1 1 0 0 1 0 1

---

Password	X value
----------	---------

---

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Recovered:            1 1 1 b y y y y b 0 y y y y b 1 1 1 b 0 y y y y b

pwd_1	1 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 1
pwd_2	1 1 0 0 1 0 1 1 1 1 1 1 0 0 0 0 1 0 1 1 1 0 1
pwd_3	0 1 1 1 0 0 0 0 0 0 0 0 1 0 0 1 0 0 0 0 1 1 0 0 0
pwd_4	1 1 1 1 1 1 0 0 0 0 1 0 1 1 0 1 1 1 0 0 0 1 1 1 1
pwd_5	0 1 1 1 1 0 1 1 1 1 0 0 1 0 1 1 1 0 0 0 0 1 0 0 0
...	
pwd_n	1 0 0 0 1 1 0 0 0 0 0 0 0 0 0 1 1 0 1 1 0 0 1 0 1

---

Password	X value
----------	---------

---

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 $v = g^x \text{ mod } p$

Rules ( $b \in \{0,1\}$ ):

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$Xx.....x \rightarrow 0 \dots 0yyyyy$

Recovered:	1 1 1 b y y y y b 0 y y y y b 1 1 1 b 0 y y y y b	
pwd_1	1 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 1	15
pwd_2	1 1 0 0 1 0 1 1 1 1 1 1 0 0 0 0 1 0 1 1 1 0 1	14
pwd_3	0 1 1 1 0 0 0 0 0 0 0 0 1 0 0 1 0 0 0 0 1 1 0 0 0	11
pwd_4	1 1 1 1 1 1 0 0 0 0 1 0 1 1 0 1 1 1 0 0 0 1 1 1 1	0
pwd_5	0 1 1 1 1 0 1 1 1 1 0 0 1 0 1 1 1 0 0 0 0 1 0 0 0	11
...		
pwd_n	1 0 0 0 1 1 0 0 0 0 0 0 0 0 0 1 1 0 1 1 0 0 1 0 1	12

---

Password	X value	Diff score
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---

# Single Measurement Attack

- Very accurate measurement
- Each bit of information halves the number of possible passwords
  - $k$  bits of information  $\Rightarrow 2^{-k}$  probability of false positive/negative

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- Each bit of information halves the number of possible passwords
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For a  $n$  bits exponent, we get  $k = 0.4n + 2$  bits on average (verified empirically)

SHA-1: 66 bits of information

SHA-256: 104 bits of information

# Practical Impact

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# Impacted Projects

- Lots of project using OpenSSL are impacted, including
  - OpenSSL TLS-SRP
  - Apple HomeKit ADK
  - PySRP (used in ProtonMail python client)
  - GoToAssit (?)

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Wait, how are big numbers managed in high level languages ?...

- Many reference libraries are based on OpenSSL to manage bignums
- They usually (never ?) manage the flag properly
  - Ruby/openssl
  - Javascript node-bignum
  - Erlang OTP

All SRP implementations using these packages / libraries would be affected!

## Mitigations & Conclusion

---

Two choices:

- Patch this particular issue by adding the proper flag
  - Most projects use the bignum API, not the whole SRP
  - Difficult to propagate
  - Root cause remains
- Switch to a secure by default implementation (flag for insecure/optimized)
  - No flag = secure implementation (potential performance loss)
  - All projects are patched at once

Two choices:

- Patch this particular issue by adding the proper flag ← OpenSSL's choice
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  - Root cause remains
- Switch to a secure by default implementation (flag for insecure/optimized)
  - No flag = secure implementation (potential performance loss)
  - All projects are patched at once

After OpenSSL, we contacted impacted to help with a patch:

- Apple HomeKit ADK
- node-bignum
- Ruby/openssl
- PySRP
- protonmail-python-client
- Erlang OTP

- Practical attack against SRP implementations
  - Vulnerability inherited by lots of projects
  - Easy to exploit because we can use each recover bits independently

Long term lesson: be careful with SCA, especially in PAKE implementation

- Practical attack against SRP implementations
  - Vulnerability inherited by lots of projects
  - Easy to exploit because we can use each recover bits independently

Long term lesson: be careful with SCA, especially in PAKE implementation

- Leakage in a weak generic function
  - Other protocols with small base may also use it
  - Contact use if you think of one!

Thank you for your attention!



<https://gitlab.inria.fr/ddealmei/poc-openssl-srp>



daniel.de-almeida-braga@irisa.fr